

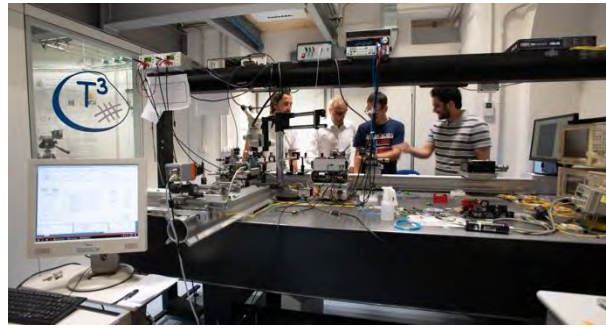


POLITECNICO
DI MILANO

Integrated photonics (The need to peep light)

Andrea Melloni

DEIB, Politecnico di Milano, Milano, Italy



Photonic Devices Lab

Andrea Melloni

Francesco Morichetti

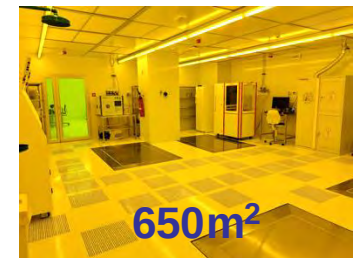
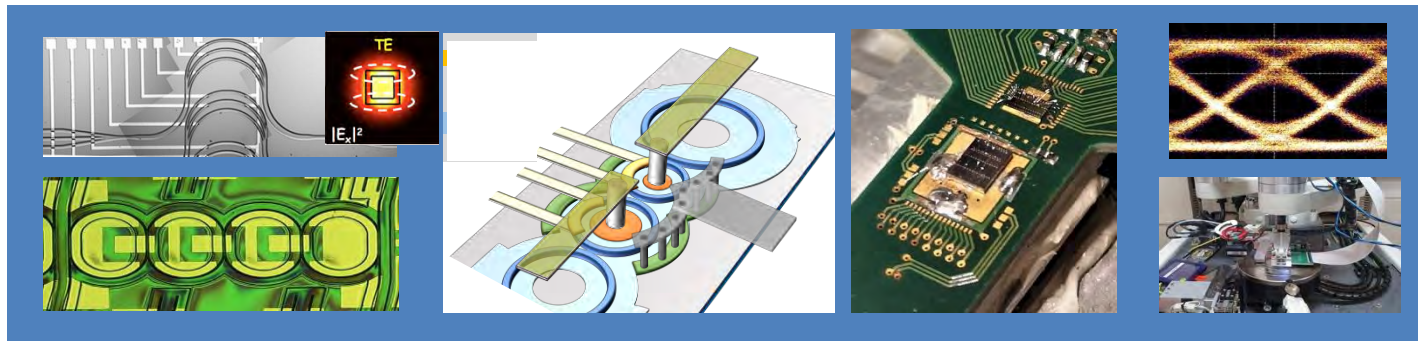
<http://photonics.deib.polimi.it>



POLITECNICO
DI MILANO

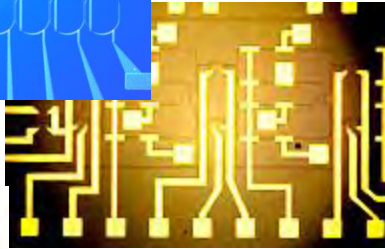


PoliMi micro- nano-
technology center

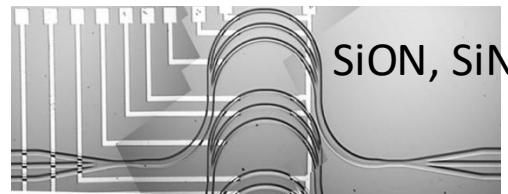
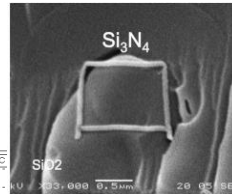
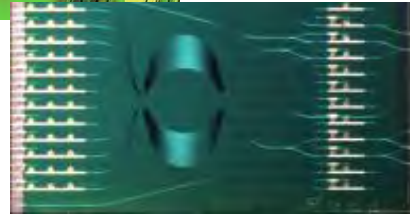




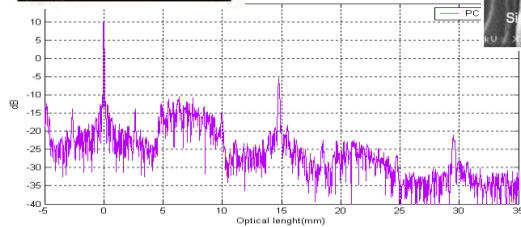
Silicon photonics



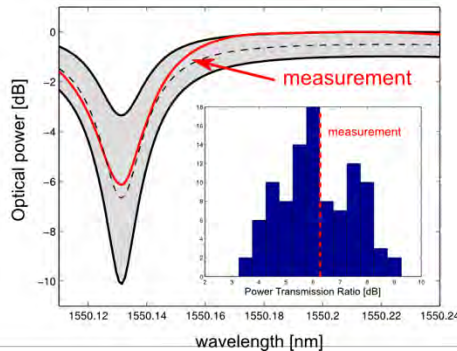
Indium phosphide



SiON, SiN

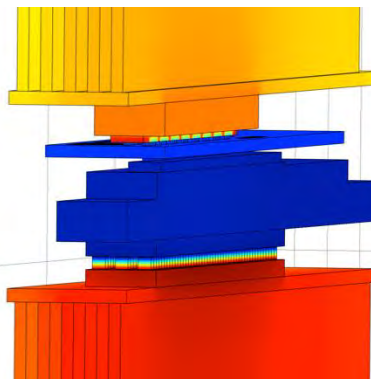


Characterization techniques

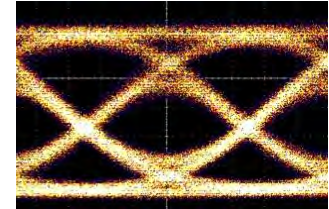
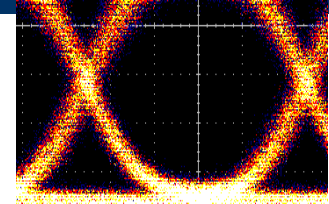


Statistical analysis

Thermal & Stress analysis

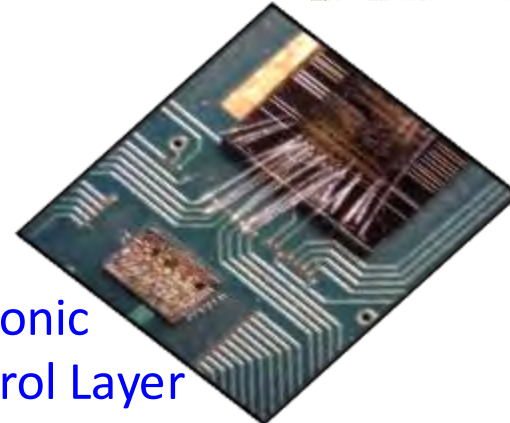
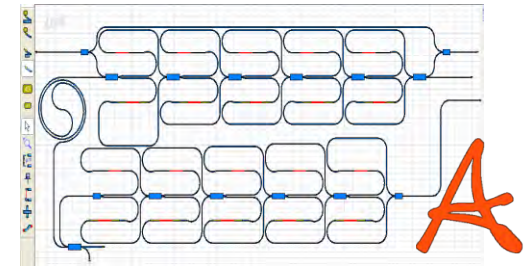


Photonic Control Layer

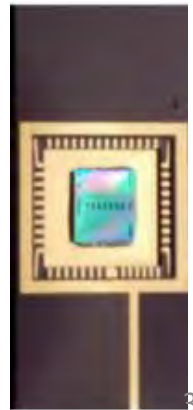


WDM up to 200 Gb/s

Commercial Circuit simulator



Biosensing





PHOTONICS²¹

Photonics

A Key Enabling Technology
for Europe

The European Technology Platform Photonics²¹ represents the photonics community of industry and research organisations. Jointly with the European Commission our members develop and implement a common photonics strategy in a Horizon2020 **Public Private Partnership (PPP)** to spur growth and jobs in Europe.

Photonics²¹ – Photonics PPP
Annual Activity Report 2017



PHOTONICS PUBLIC PRIVATE PARTNERSHIP

PHOTONICS²¹



Europe's age of light!

How photonics will power
growth and innovation

2020-2030

Download from:
<https://www.photonics21.org>

PHOTONICS²¹

2. Photonics Research and Innovation Challenges

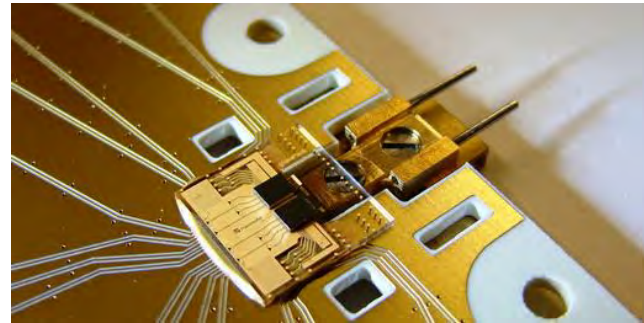
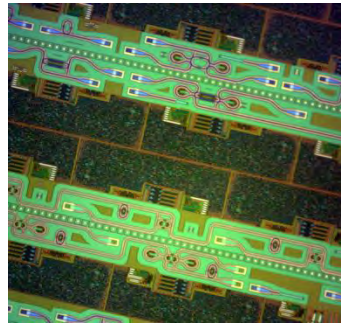
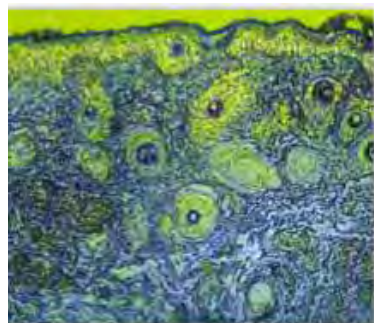
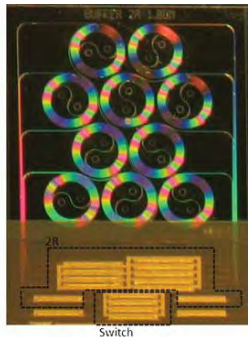
18

- | | | |
|-----|--|----|
| 2.1 | Information & Communication | 18 |
| 2.2 | Industrial Manufacturing & Quality | 35 |
| 2.3 | Life Science & Health | 41 |
| 2.4 | Emerging Lighting, Electronics & Displays | 49 |
| 2.5 | Security, Metrology & Sensors | 60 |
| 2.6 | Design and Manufacturing of Components & Systems | 70 |
| 2.7 | Education, Training & Disruptive Research | 83 |

Photonics

A Key Enabling Technology for Europe

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Polifab - the micro and nano fabrication facility of PoliMI

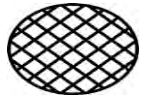


Polifab provides **high technological standards** for a wide range of applications: photonics, micro and nanoelectronics, MEMS, biotechnologies, advanced materials and nanotechnology.

Polifab acts as an **aggregating** center for academic researchers, start-ups and companies



+600 mq cleanroom, ISO 06



Up to 200 mm wafers



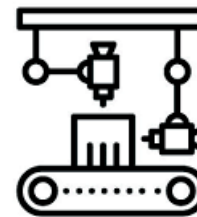
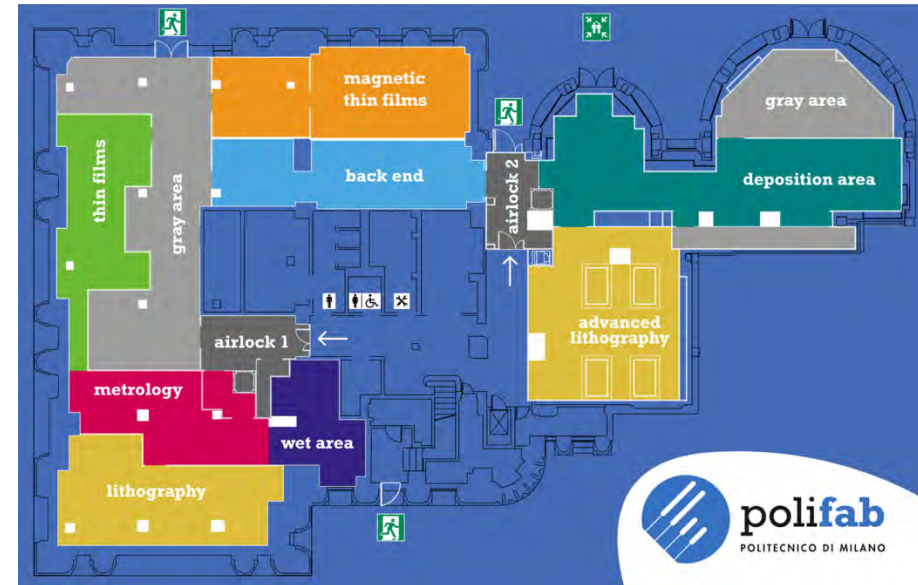
11 staff members



Open access



+160 researchers in 2024



~ 25 M€ tools installed

~ 40% from JRC with STm

Multidisciplinary approach, flexibility

Lithography

Photolithography
2 Maskless photolitho
Electron beam lithography 50keV
Thermal scanning lithography

Deposition

Electron beam evaporation
Thermal evaporation
Sputtering for metals and oxides
Chemical vapor deposition
Electrodeposition
ALD

Etching

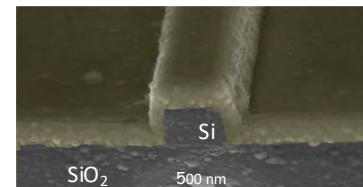
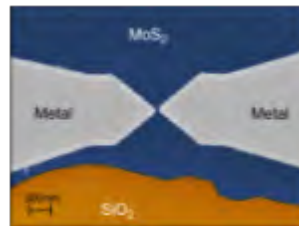
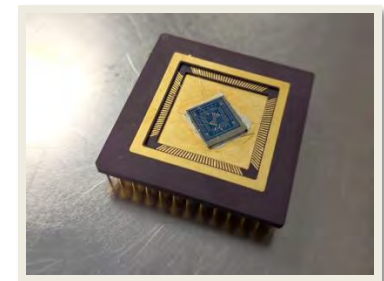
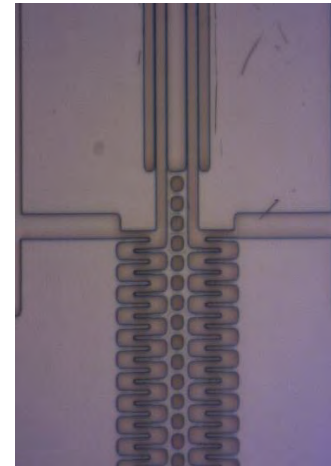
Reactive ion etching
Deep RIE
Ion beam etching
Plasma ashing
Wet etching
Lift-off

Characterization

Optical microscopy
Stylus profilometry
Optical profilometry
SEM, AFM
Ellipsometry
Electrical measurements
X-ray diffraction
EDX
Micro-Raman spectroscopy

Backend

Annealing ovens
Rapid thermal annealing
Wire bonding
Dicing
Pick & Place
Alignments tools
Two-photon polymerization tool



<http://www.polifab.polimi.it>

Contents

- ✓ (short) Overview on integrated photonics
- ✓ The photonic chip as system
 - ✓ Monitors
 - ✓ Actuators
 - ✓ (Feedback and Control)
- ✓ Applications: routing, tuning and computing



THE BELL SYSTEM TECHNICAL JOURNAL

DEVOTED TO THE SCIENTIFIC AND ENGINEERING
ASPECTS OF ELECTRICAL COMMUNICATION

Volume 48 September 1969 Number 7

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Integrated Optics: An Introduction

By STEWART E. MILLER

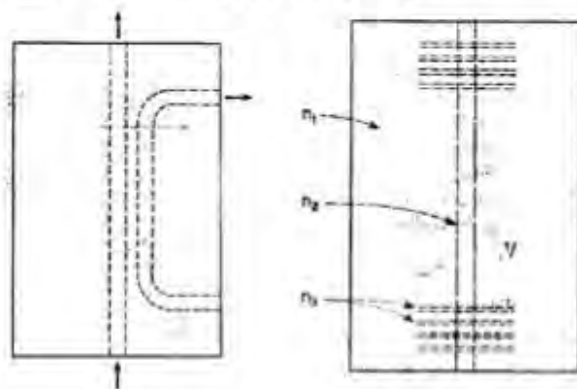


Fig. 6—Directional coupler type hybrid. (a) Resonator using planar waveguide.

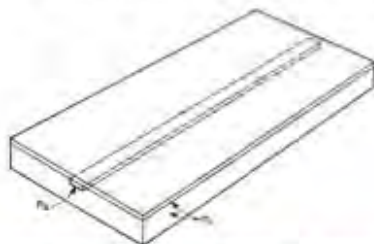


Fig. 7—Planar waveguide formed using photolithographic techniques.

Bends in Optical Dielectric Guides

By E. A. J. MARCATILI

(Manuscript received March 3, 1969)

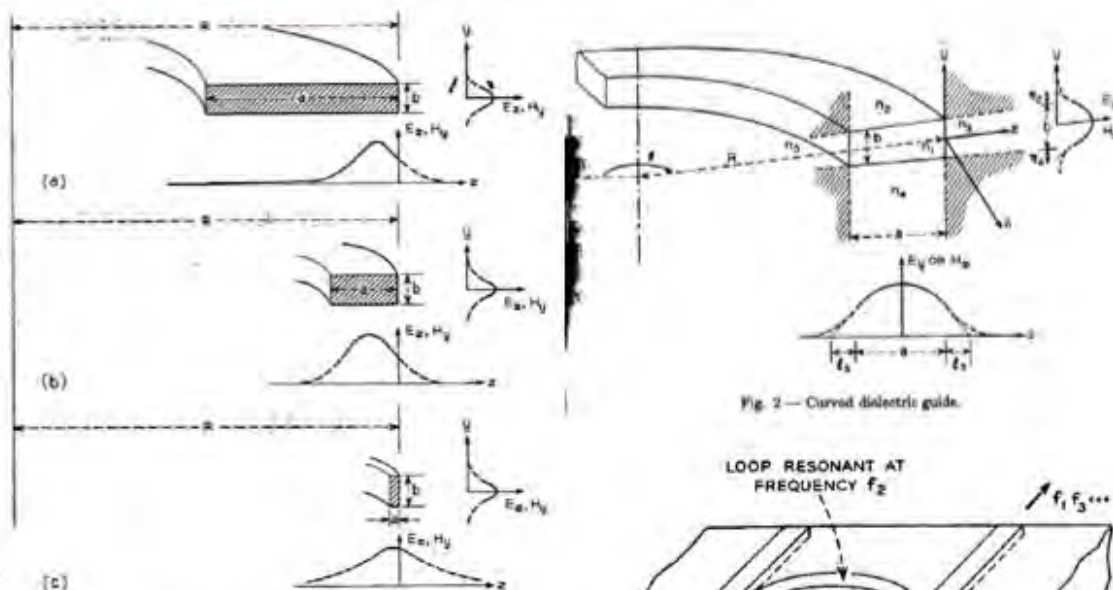


Fig. 6—Field distribution as a function of guide width a with (a) $a/A > 1$, (b) $a/A \approx 1$, and (c) $a/A < 1$.

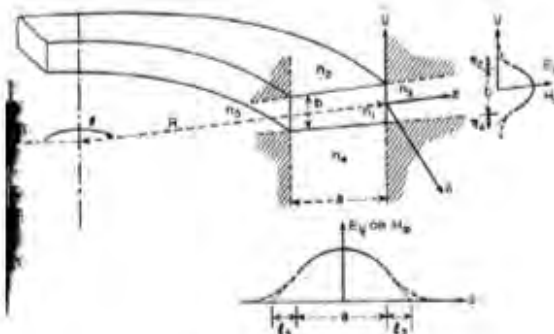


Fig. 2—Curved dielectric guide.

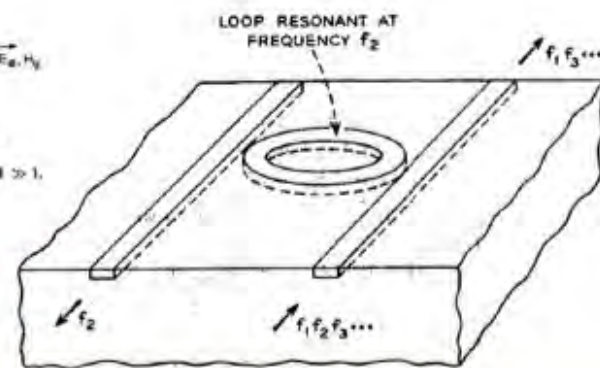
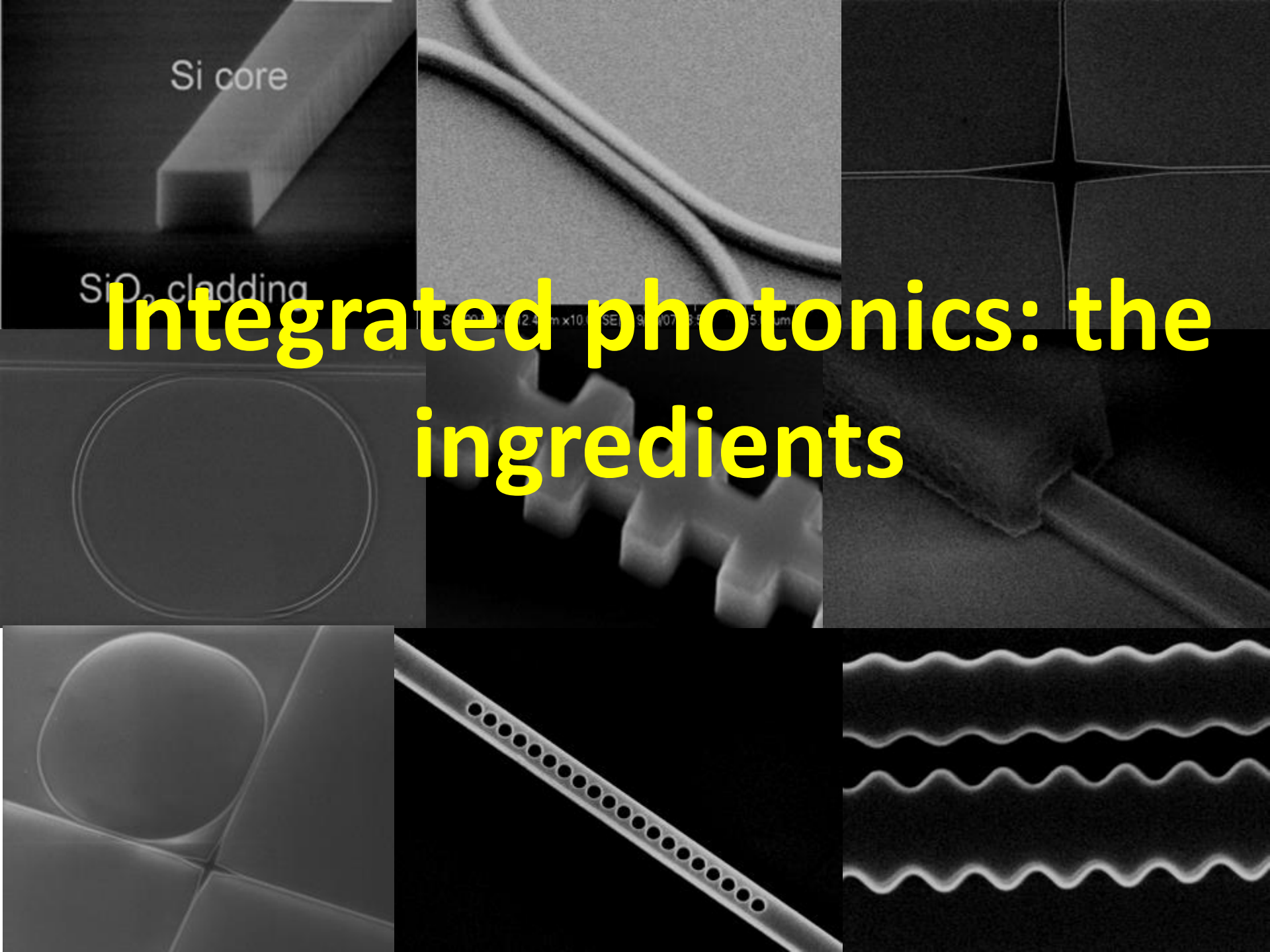


Fig. 1—Channel dropping filter (ring type).

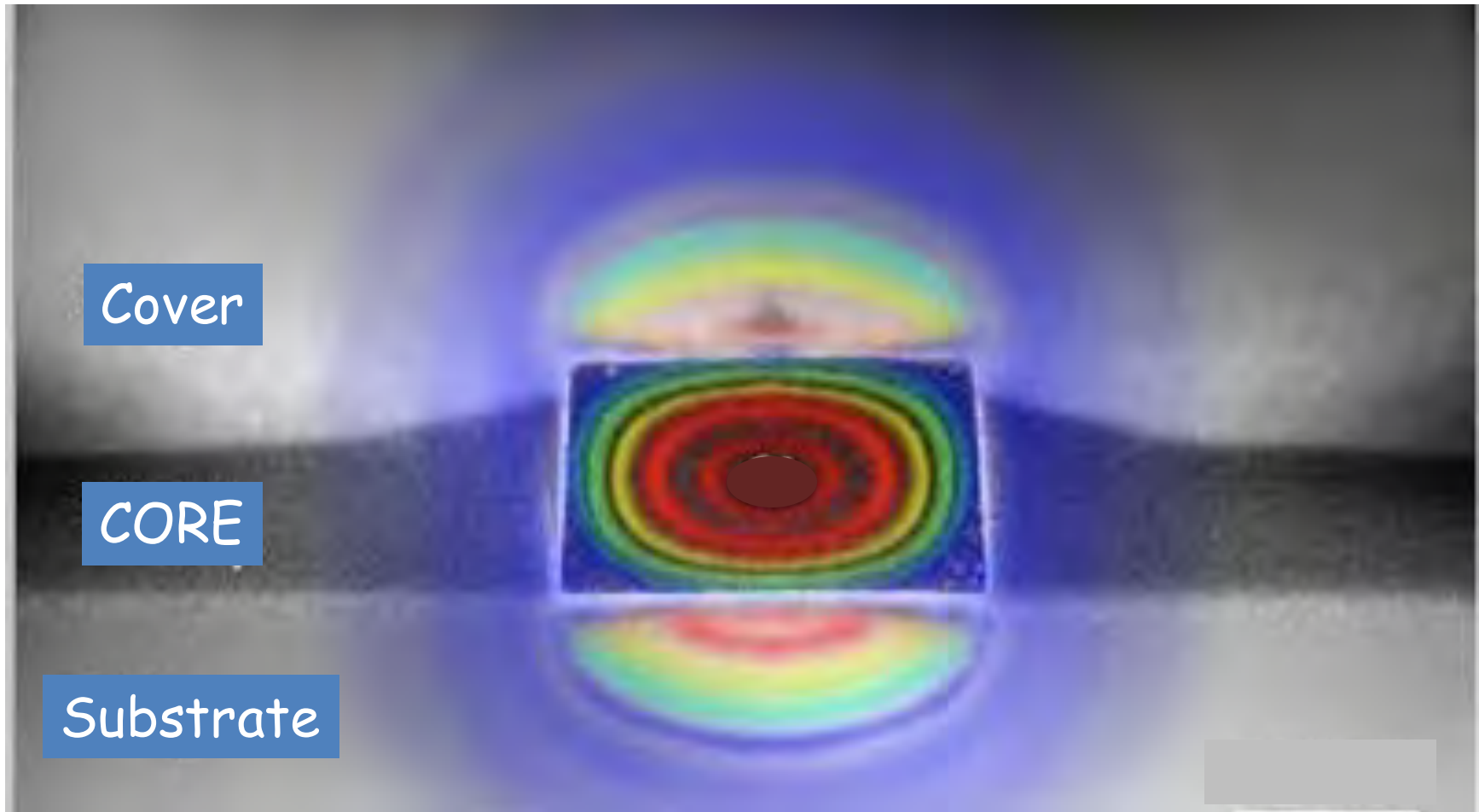
Si core

SiO₂ cladding

Integrated photonics: the ingredients



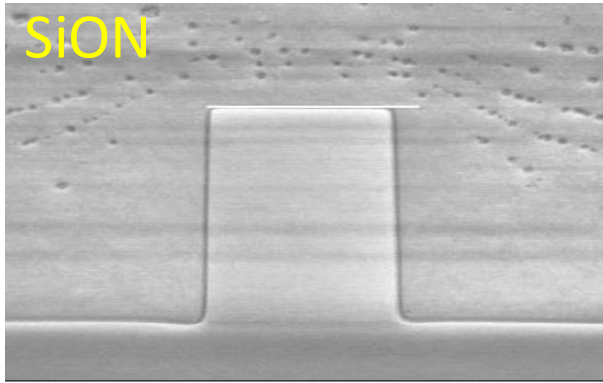
WAVEGUIDE



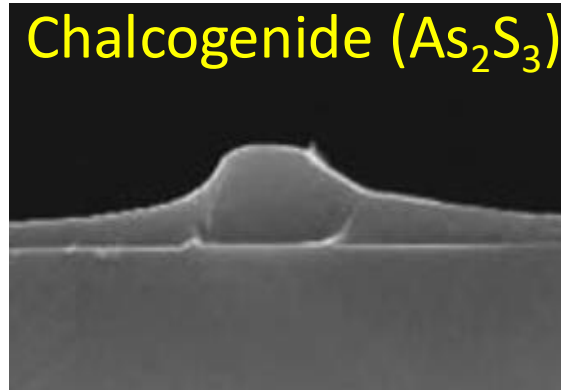
Waveguides...



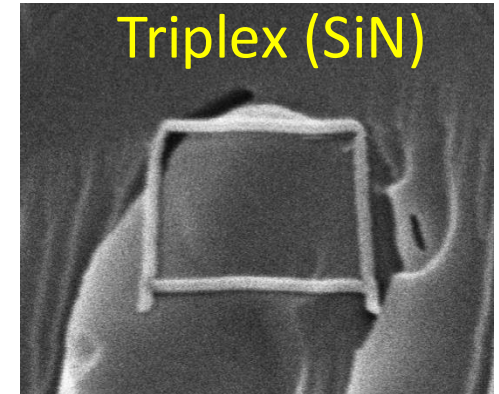
SiON



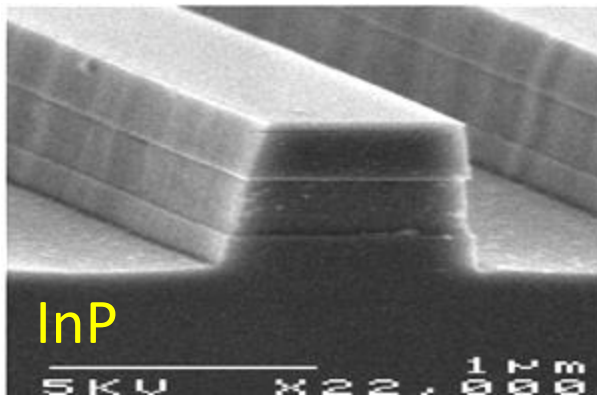
Chalcogenide (As_2S_3)



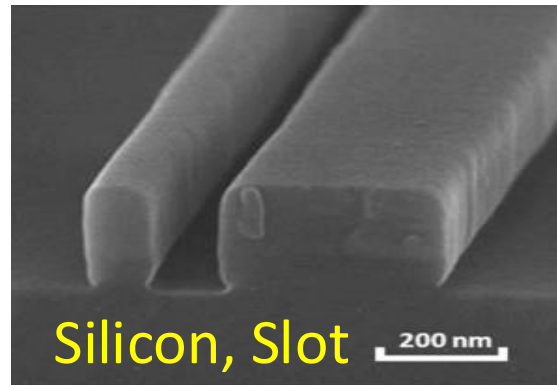
Triplex (SiN)



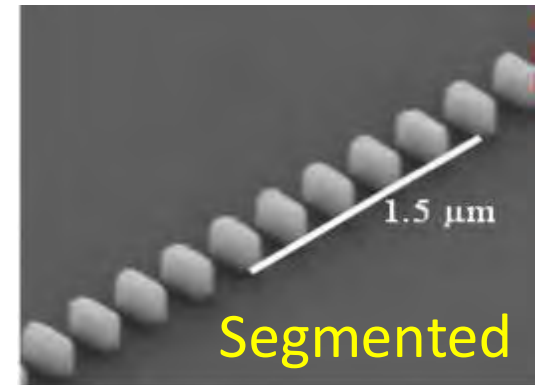
InP



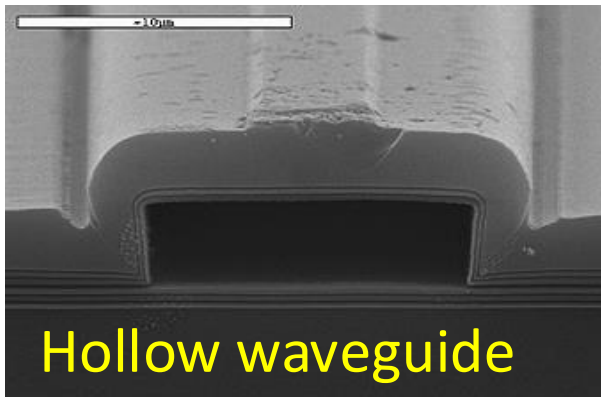
Silicon, Slot



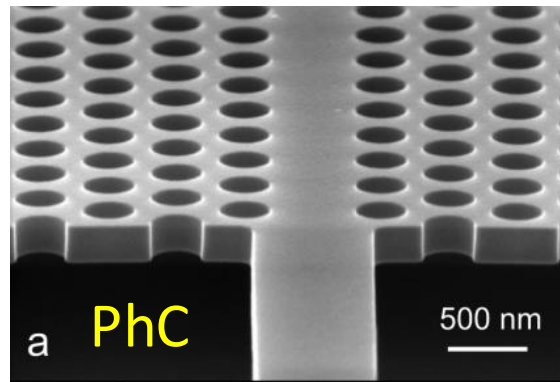
Segmented



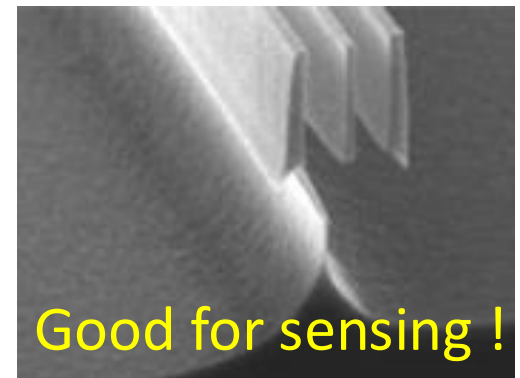
Hollow waveguide



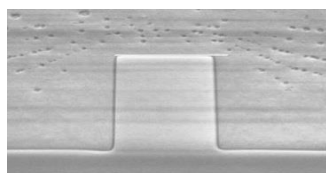
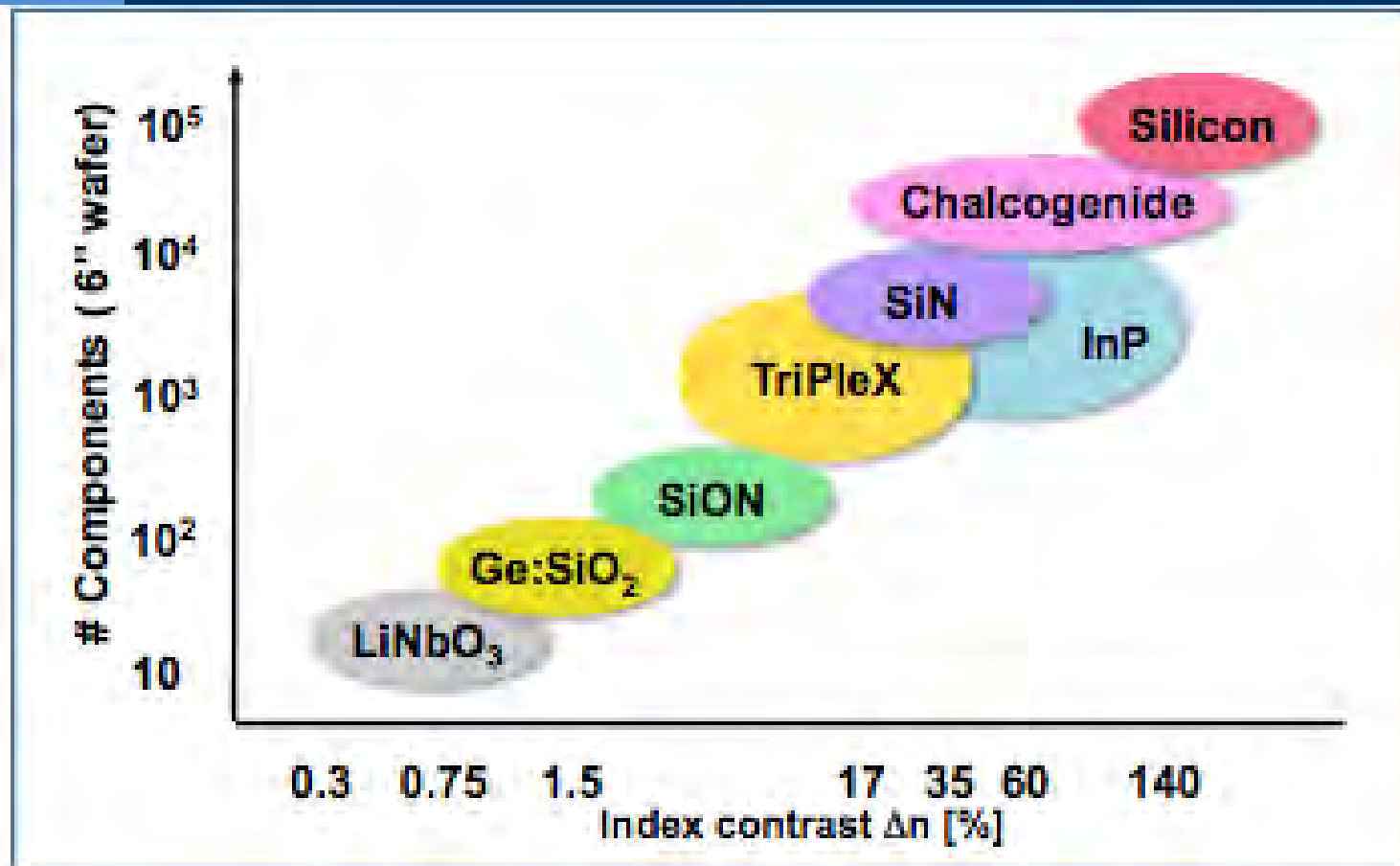
a PhC



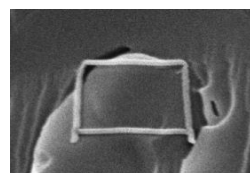
Good for sensing !!



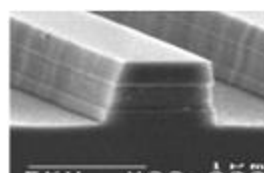
Materials for Photonic circuits



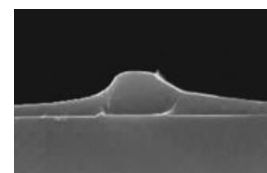
Ge:SiO₂
0.5...3 %



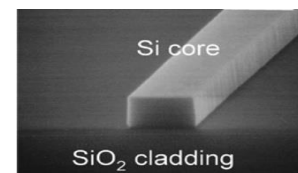
SiON
2...8 %



Si₃N₄
38 %



InP
3 / 70 %

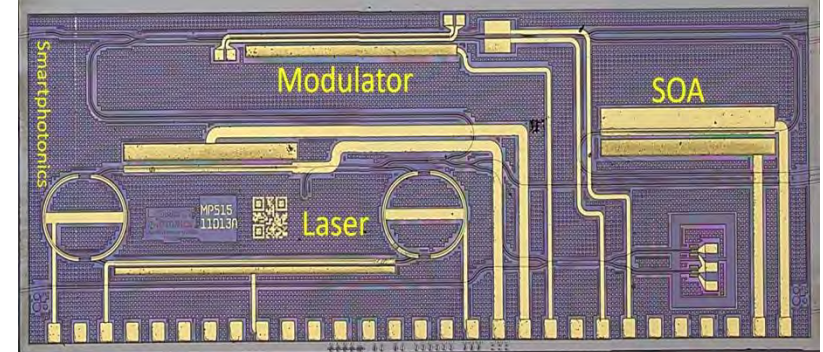
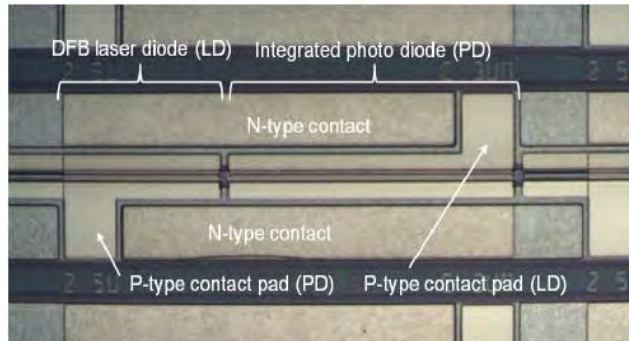
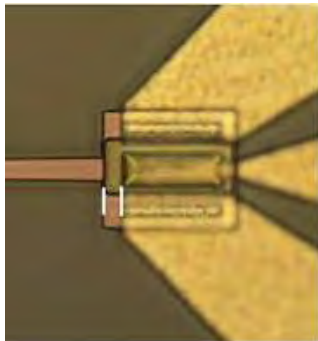
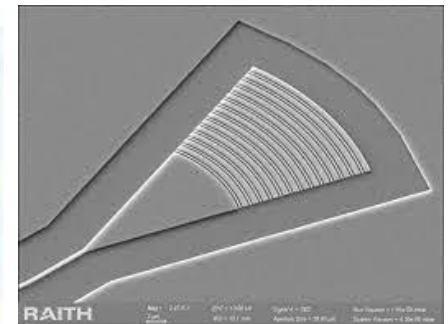
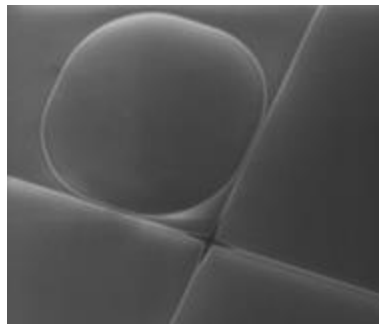
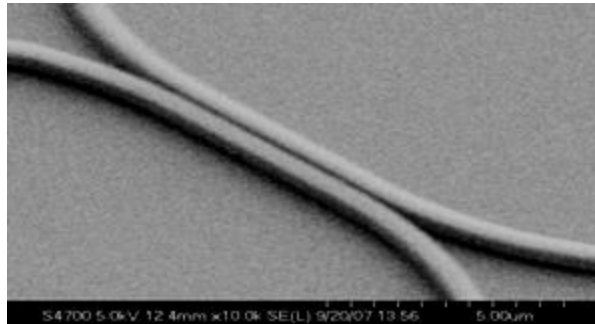
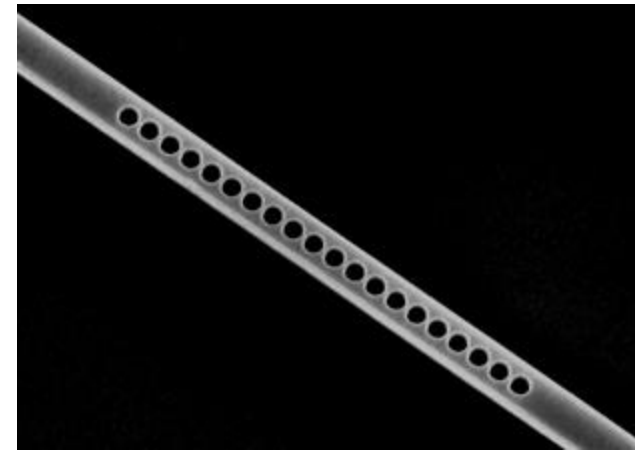
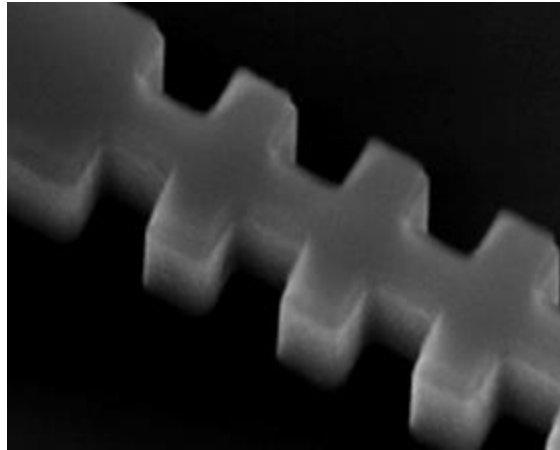
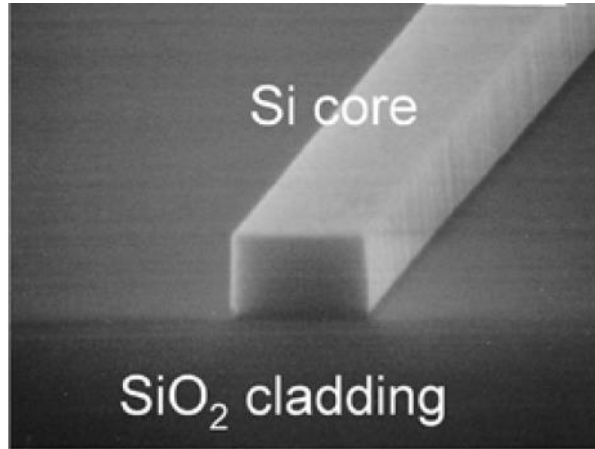


As₂S₃
60...100 %

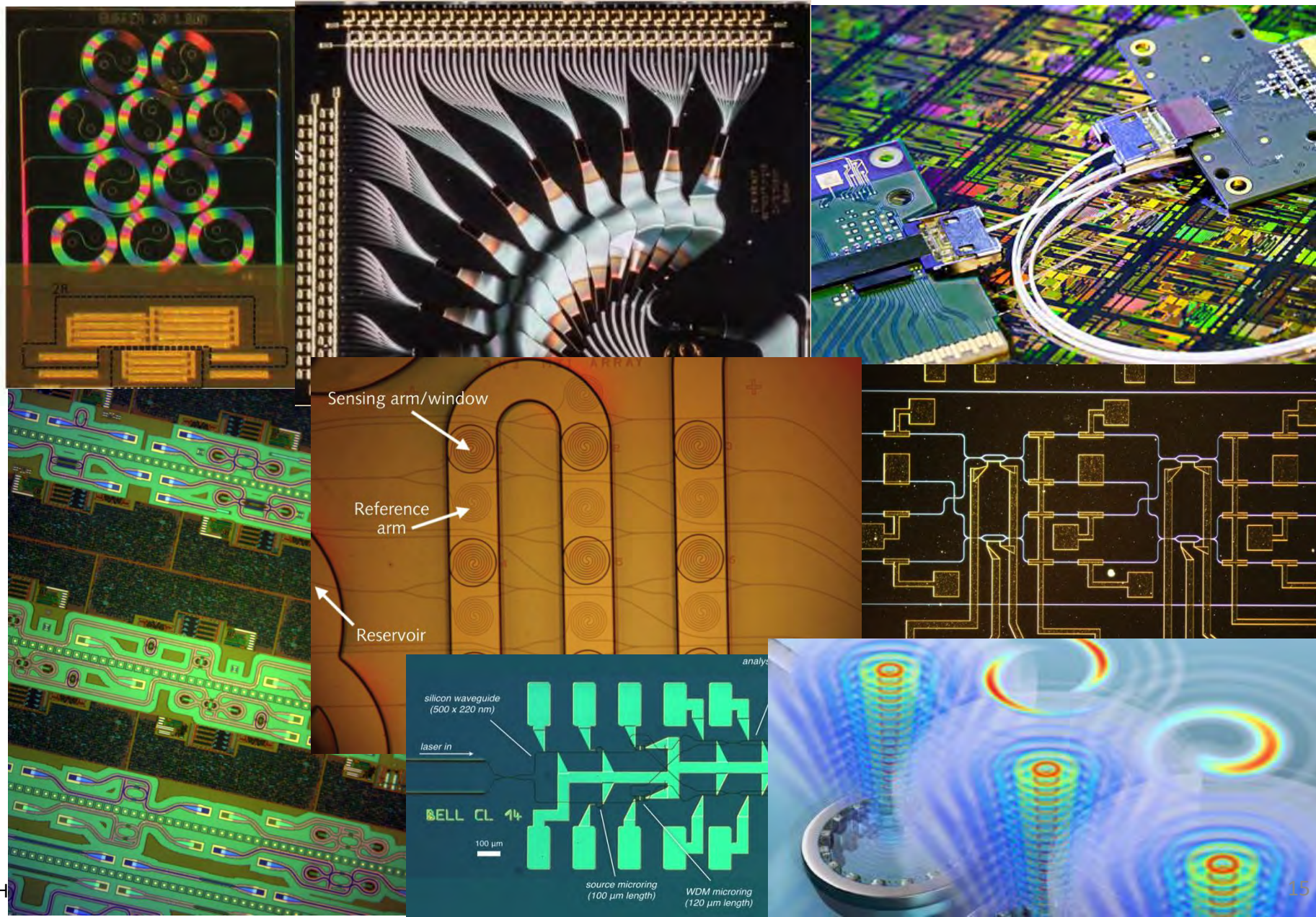
Silicon
140%

Δn

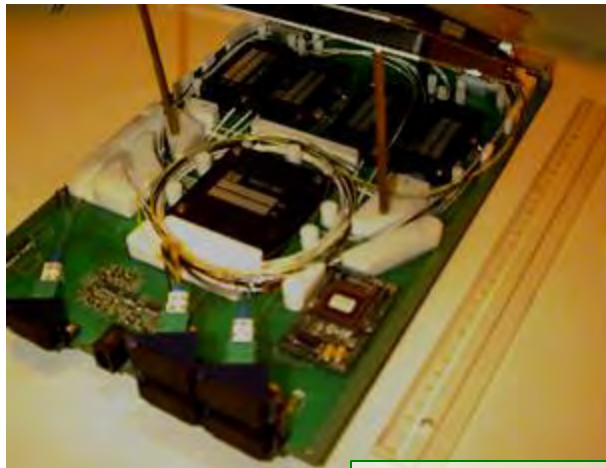
Integrated Photonics Building Blocks



Integrated photonics: towards ubiquitousness

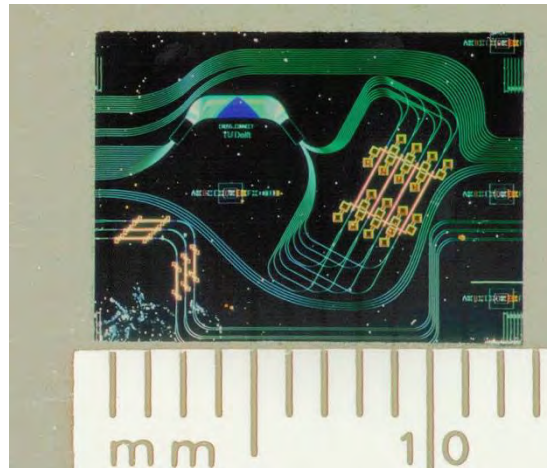


The need of Integrated Photonics



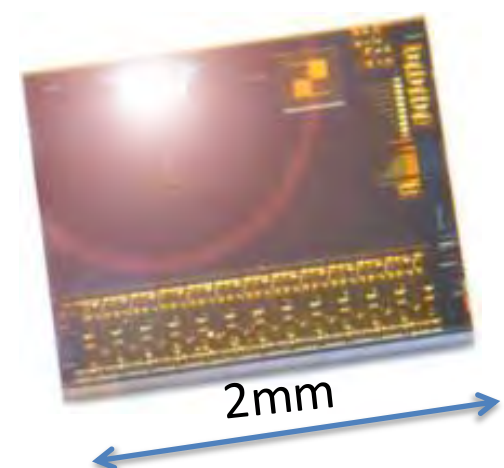
1994

4- λ 2x2 OXC



1998

4- λ 2x2 OXC

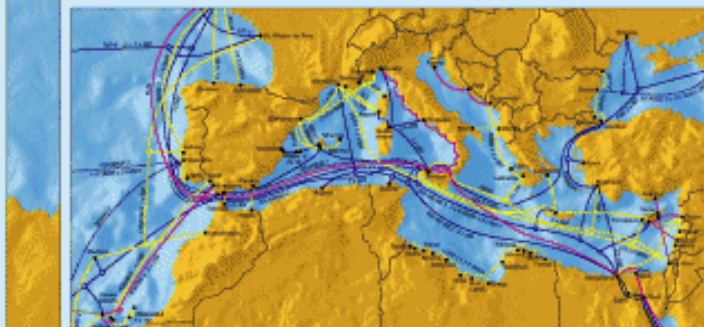
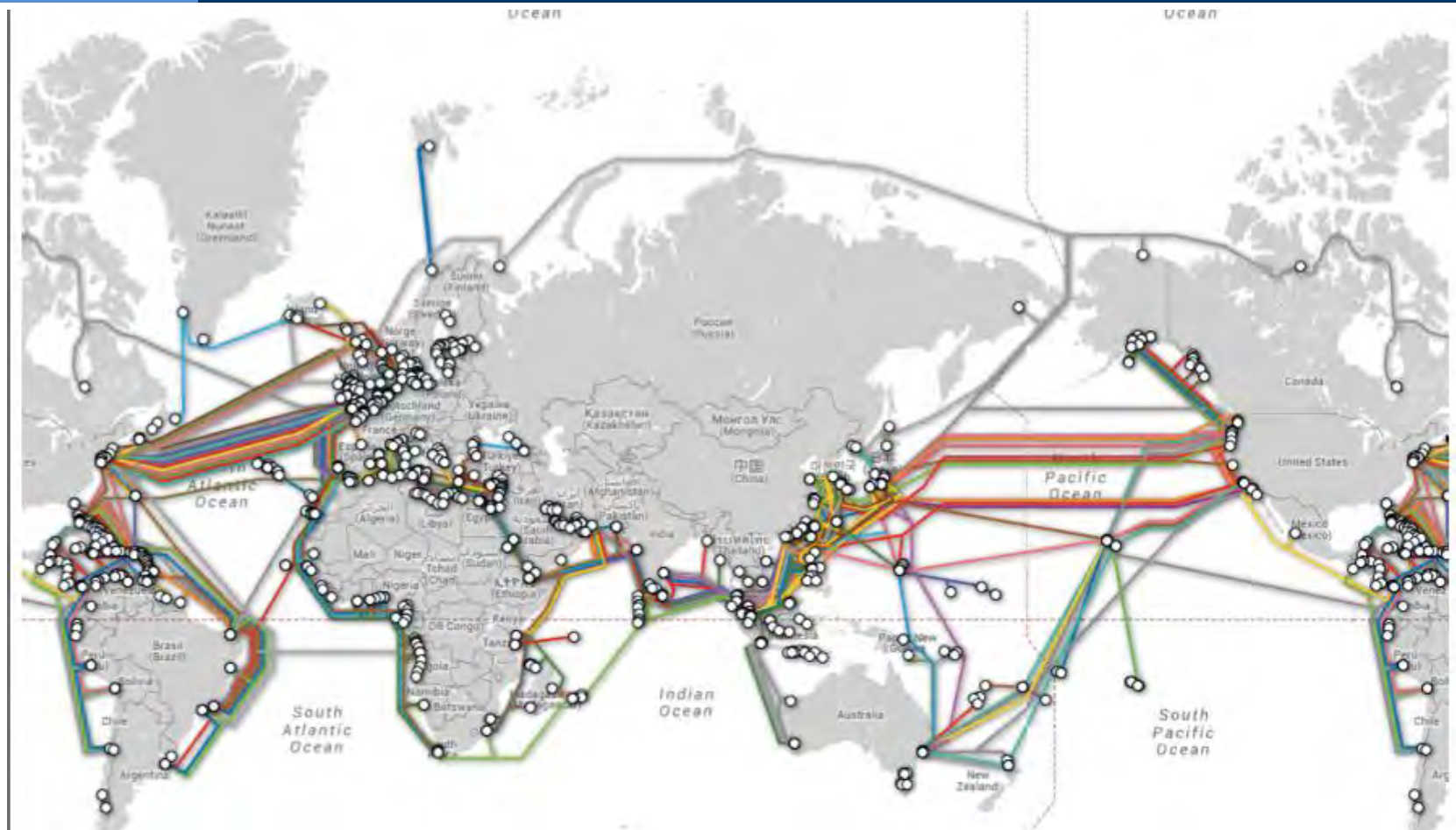


2018 Transceiver
2.4Tb/s, 12000km



- Greatly reduced component cost
 - Monolithic interconnection of device elements
 - Simpler packaging and assembly, standard processes
- High reliability
 - Less interfaces
- High functionality
 - Many more functional elements per chip, higher creativity in design
- High phase stability, excellent device matching
 - Permits interferometric structures
- Robust
 - Single chip designs with minimal optical interfaces are ideal for demanding environments
- Higher power efficiency
 - Minimize optical power loss at interfaces between device elements
- Reduce packaging costs
- Co-integration with electronic, microfluidic, MEMS, microwave,
- Volume production

Submarine cables, optical fibers

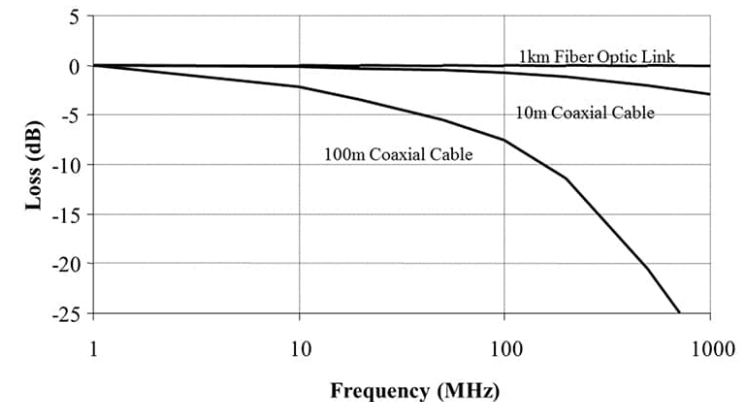


Why optical fibers?



- **Data Rate:** Optical fibers support **Tbps speeds**, copper cables are limited by high frequency metallic loss (**no skin effect**)
- **Longer Distance:** Optical fibers can transmit data over many km without significant signal loss.
- **Power Consumption:** Optical transceivers consume **less power per bit** than copper alternatives, making them **more energy-efficient**
Optical fibers generate **less heat** than high-speed copper cables.
- **Latency:** Optical signals travel at **near the speed of light (both in fibers and copper cables !... See table)** – Hollow core fibers?
- **Electromagnetic Interference (EMI):** optical fibers are **not affected by EM noise**, ensuring **signal integrity** in high-density environments (like thousands of servers)
- **Space & Weight:** Optical fibers are **thinner and lighter** than copper cables, **better airflow and cooling**

Loss v Frequency Comparison for Fiber & Coaxial Cable



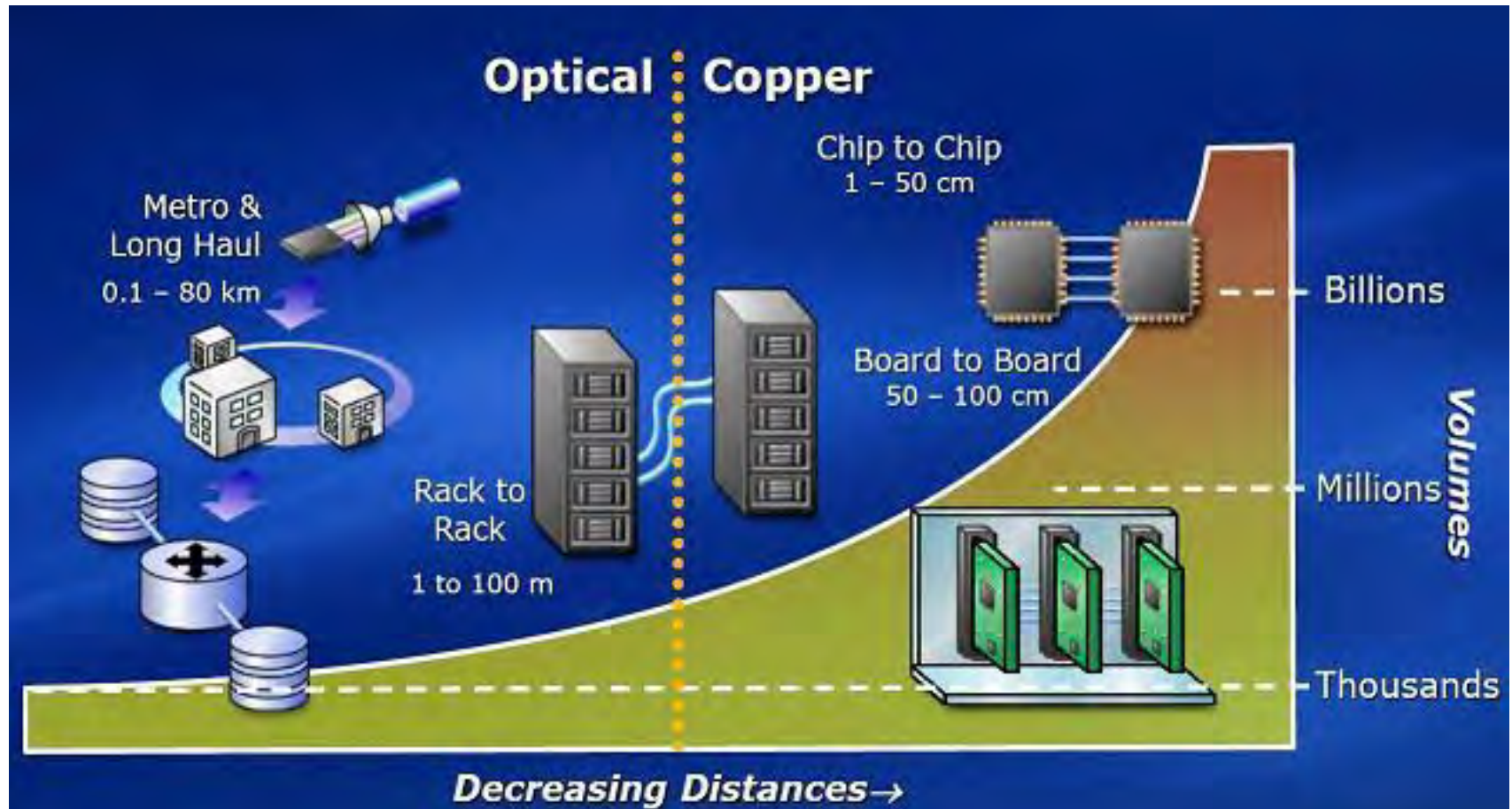
Material	Dielectric constant	VOP
TYPICAL INSULATION MATERIALS		
Cellular TFR	1.38	85%
FEP	2.1	69%
Silicone	3.6-2.1	53-69%
TFE	2.1	69%
Polyethylene	2.3	66%
PVC	8.2-3.0	35-58%
Nylon	4.5-3.6	47-53%
Optical fiber	2.1	70%

Velocity of propagation (VOP)

$$VOP[\%] = \frac{v}{c}$$

c speed of light (vacuum)

Photonics in datacenters & AI infrastructures...



Photonics in datacenters & AI infrastructures...

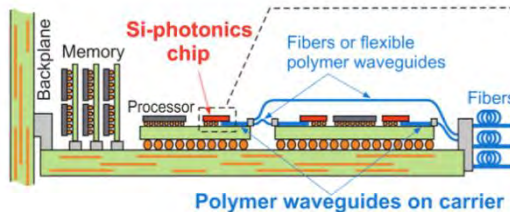


Today

Optical Transceivers

Convert electrical signals from GPUs, CPUs, and switches into optical signals for high-speed data transmission.

400G–800G today, moving toward **1.6T** optical links in near future.



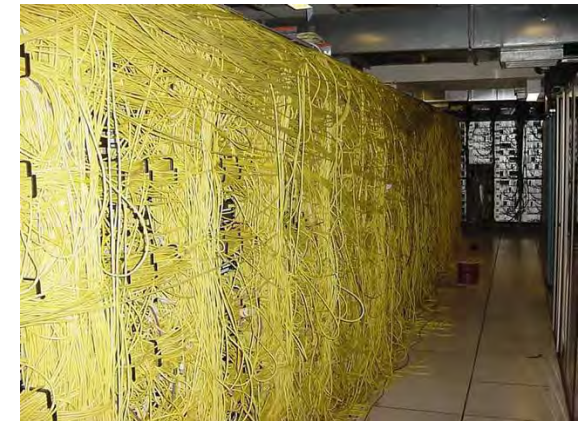
Optical Fibers Today

Intra-Rack Communication (< 2 m) → **Multimode** fibers replacing copper cables

Inter-Rack Communication (< 50 m) → **Multimode** fibers

Inter-cluster Networking (100 m – 10 km) → **Single-mode** fibers

Inter Data Center Links (50 km – 1000+ km) → **Single-mode** fibers



Optical Switches (Silicon Photonics & DWDM)

Tomorrow (< 5 years)

Use **photonic switching** to manage massive AI workloads more efficiently than electrical packet switches

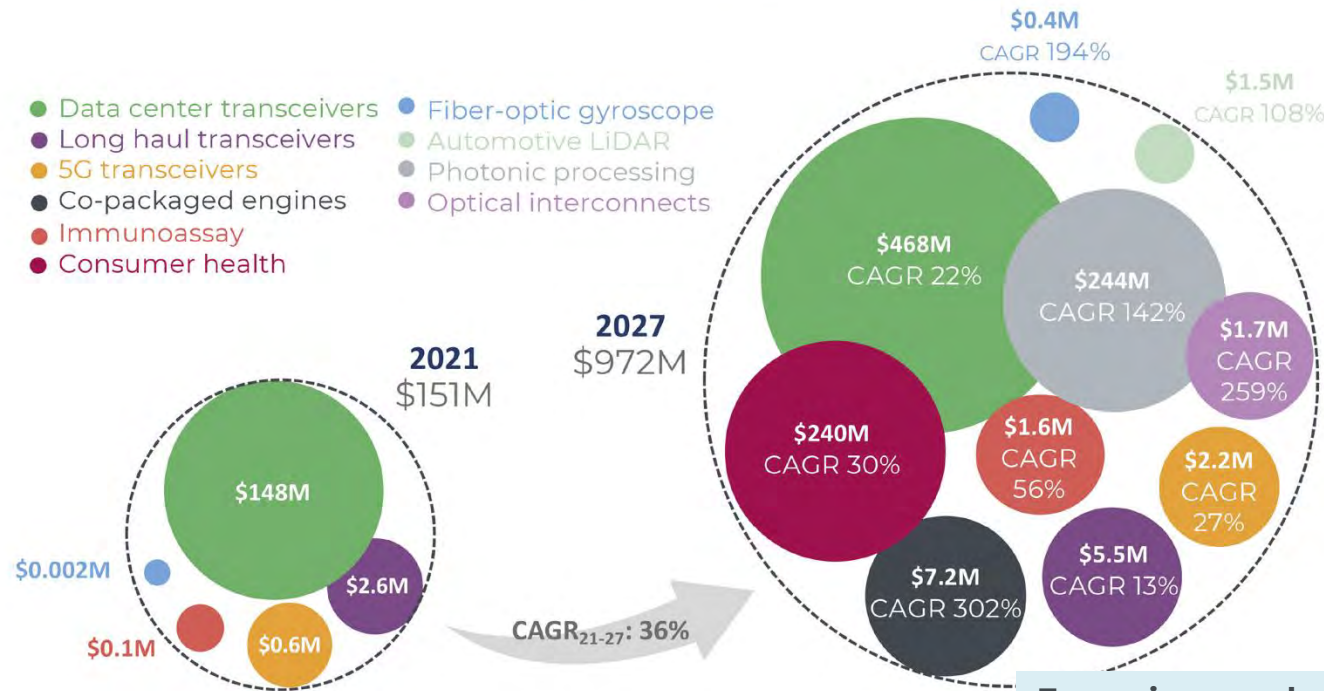
- < 50 ns switching time (faster than electrical packet switches).
- No electrical-to-optical conversion overhead (direct optical switching).





2021-2027 SILICON PHOTONIC DIE FORECAST BY APPLICATION

Source: Silicon Photonics 2022 Report, Yole Intelligence, 2022



Datacom is main market

(20% transceiver → 30% by 2027)

Emerging markets:

- medical & biosensing
- disaggregated data centers
- high-performance computing (HPC)
- analog artificial intelligence (AI)
- automotive (LiDAR and gyroscopes)
- Co-Packaged Optics engines
- ...



Optical «processors» (photonic computing)

- Reduce latency, power consumption, and bandwidth bottlenecks
- Integration of optical components (lasers, waveguides, modulators, photodetectors) directly into GPUs, TPUs...
- Optical interconnects between GPUs and memory connections (inside servers)
- Use light for (some) AI computations (photonic accelerators) → Lower energy, faster speeds
- Quantum photonic processors

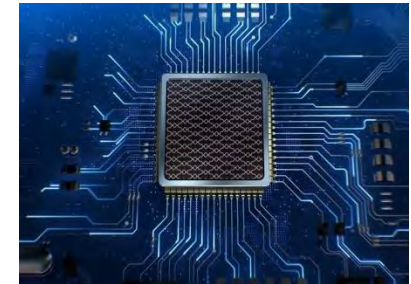
HPC wire

Since 1987 - Covering the Fastest Computers in the World and the People Who Run Them

- Home
- Technologies
- Sectors

Researchers Develop Novel Analog Processor for High Performance Computing
August 30, 2021

Aug. 30, 2021 — Analog photonic solutions offer unique opportunities to address complex computational tasks with unprecedented performance in terms of energy dissipation and speeds, overcoming current limitations of modern computing architectures based on electron flows and digital approaches.



Billions of \$ of investments.... (< 10 year old company)



<https://lightmatter.co/>



<https://ayarlabs.com/>



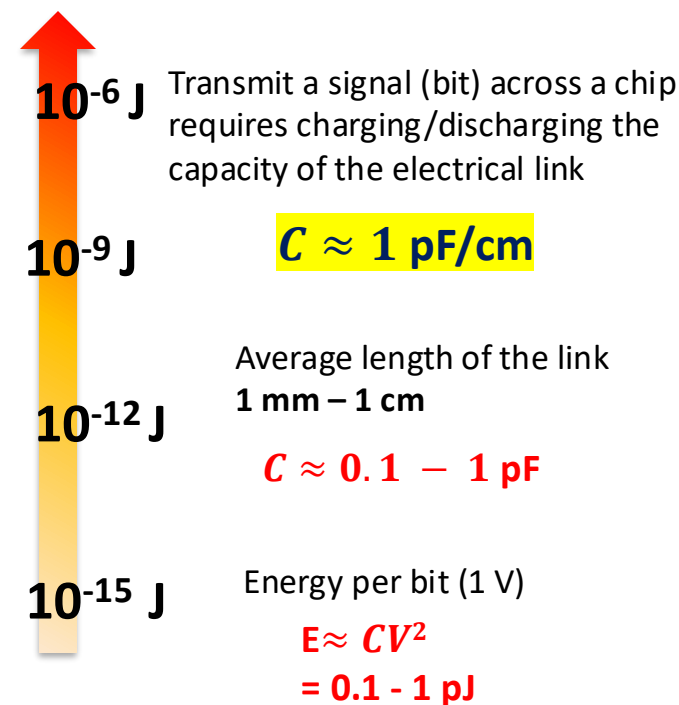
<https://www.celestial.ai/>



<https://www.psiquantum.com/>



Operation	Energy per bit
Wireless data	10 – 30 μ J
Internet: access	40 – 80 nJ
Internet: routing	20 nJ
Internet: optical WDM links	3 nJ
Reading DRAM	5 pJ
Communicating off chip	1 – 20 pJ
Data link multiplexing and timing circuits	$\sim$ 2 pJ
Communicating across chip	600 fJ
Floating point operation	100 fJ
Energy in DRAM cell	10 fJ
Switching CMOS gate	$\sim$ 50 aJ – 3 fJ



- Energy required to transmit data across electronic chips has not scaled down much in the last years
- Energy consumption of (super)computers is mainly due to short-distance signal transmission inside electrical chips

David A. B. Miller, "Attojoule Optoelectronics for Low-Energy Information Processing and Communications», J. of Lightwave Technology 35(3), Feb. 2017

Energy consumption of hyperscale computing

10^{23} FLOP/Day

GPT-4



Supercomputers can achieve **hundreds of peta FLOPS** (floating point operations per second) in processing data

FLOP/s = 10^{18} FLOP/s (# FLOP/day $\approx 10^{23}$)

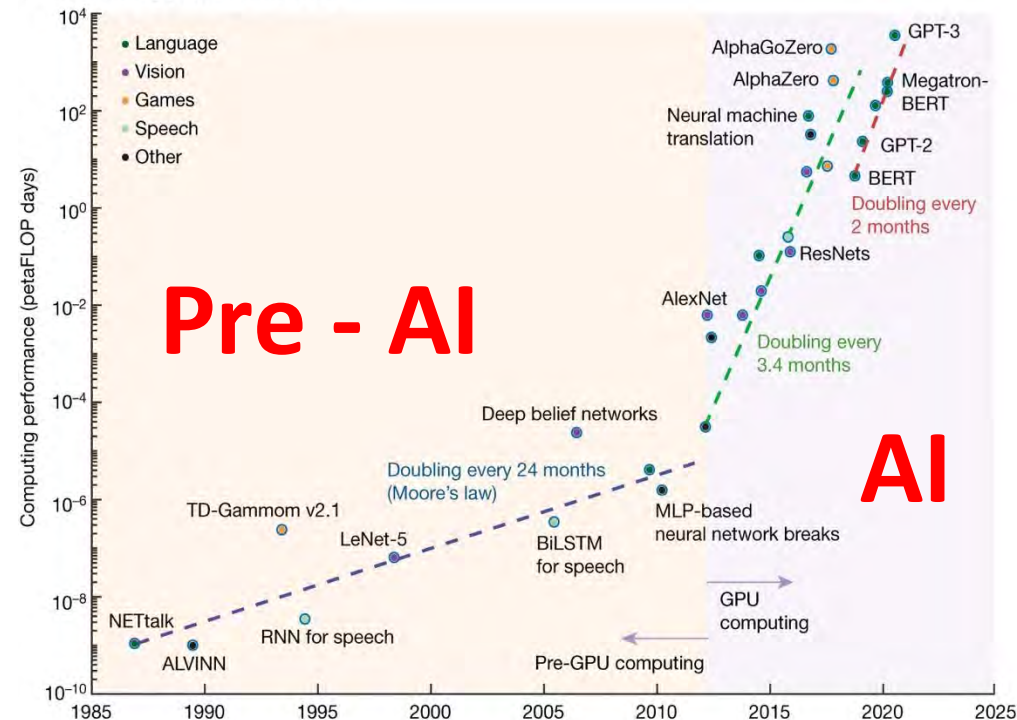
Energy per FLOP & Communication $E_{\text{FLOP}} = 1 - 10 \text{ pJ}$

Total power consumption $>10 \text{ MW}$

New computing technologies ($\rightarrow$ «Silicon» Photonics)

- Remove (or reduce) energy consumption associated with data transmission and processing in digital electronics
- Transmit and compute in the optical domains

a Computing power demands



Attojoule Optoelectronics for Low-Energy Information Processing and Communications

David A. B. Miller, *Fellow, IEEE, Fellow, OSA*

[13], [14]. But, now we are facing a need to have optics help at shorter distances, and not just to enable higher interconnect densities. Now a key question is whether optics can reduce energy in interconnects inside cabinets, racks, and circuit boards, down at least to the edges of the chips themselves, and possibly even on the chip. This question is critical: if we cannot solve these problems with optics, it is not clear that we have any other way of tackling them.

D.A.B. Miller, "Attojoule Optoelectronics for Low-Energy Information Processing and Communications", J. of Lightwave Technology 35(3), Feb. 2017

What can we do (easily & conveniently) in photonics?



Function	Electronics	Photonics
MAC & MVM	CV ² Energy Cost	Easy
Communication		Free
Gain	Easy	Easy (but off-chip)
Nonlinearity	Easy (Transistor)	Hard
Memory	Easy (DRAM, SRAM)	Hard

In neural networks, the convolutional part based on MVM occupies > 80% of the total processing time

$O(N^2)$

$O(N)$

Matrix-vector multiplication (MVM) & multiplications & accumulation (MAC) is everywhere in data processing:

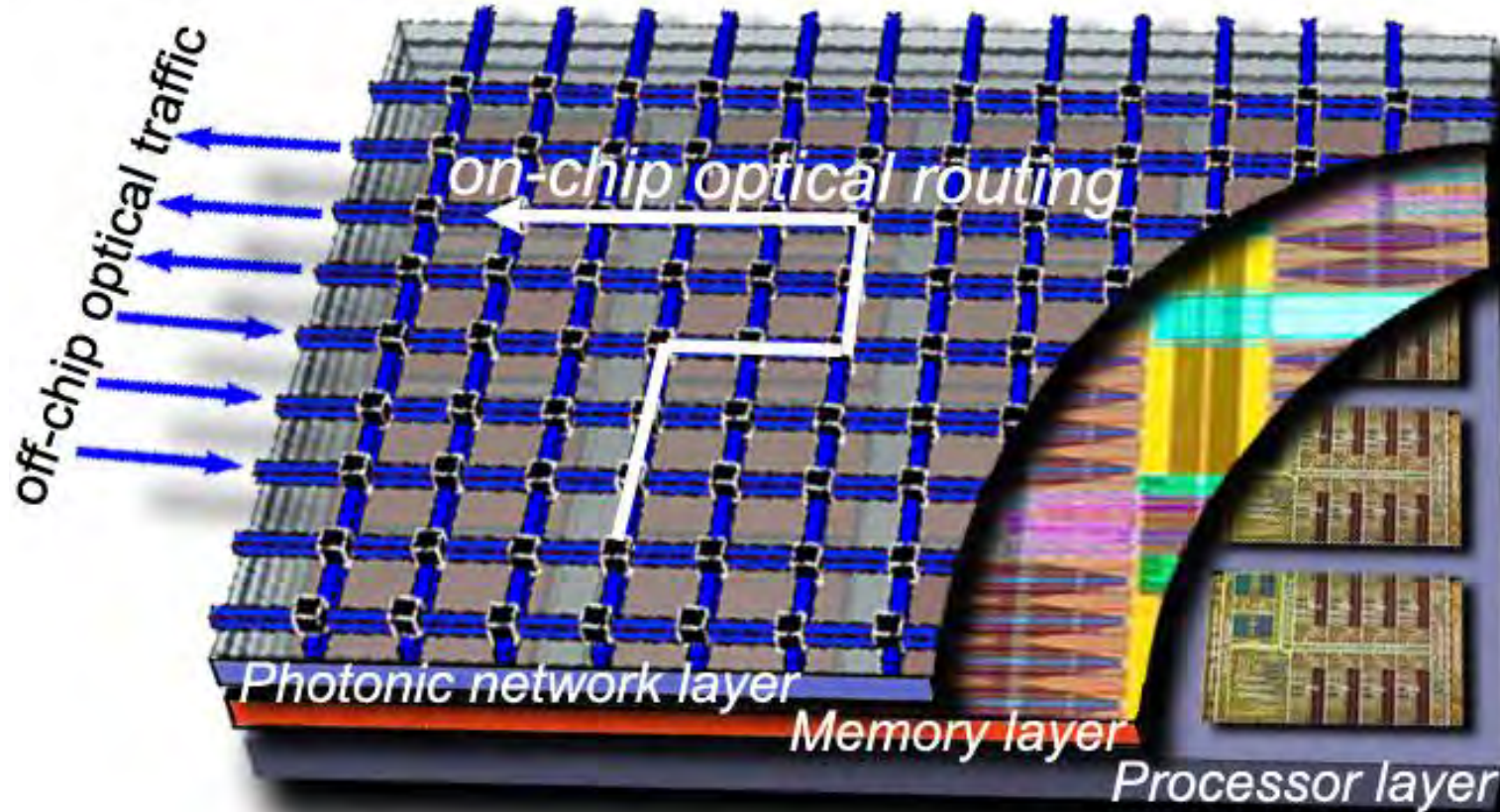
- convolution, factorization, linear equalization, filtering, Fourier transform...
- neuro-inspired computing (weighted interconnections between adjacent photonic neurons)

Advantages of photonic computing

- high speed (THz) & low latency (< ns) in solving linear mathematical operations
- low energy/bit consumption (<< pJ/bit)

- optical computing is a competitive candidate for **artificial intelligence accelerators**
- acceleration is achieved by matching math operations and photonic hardware

Photonics Integration – Optical interconnect



IBM, 2008

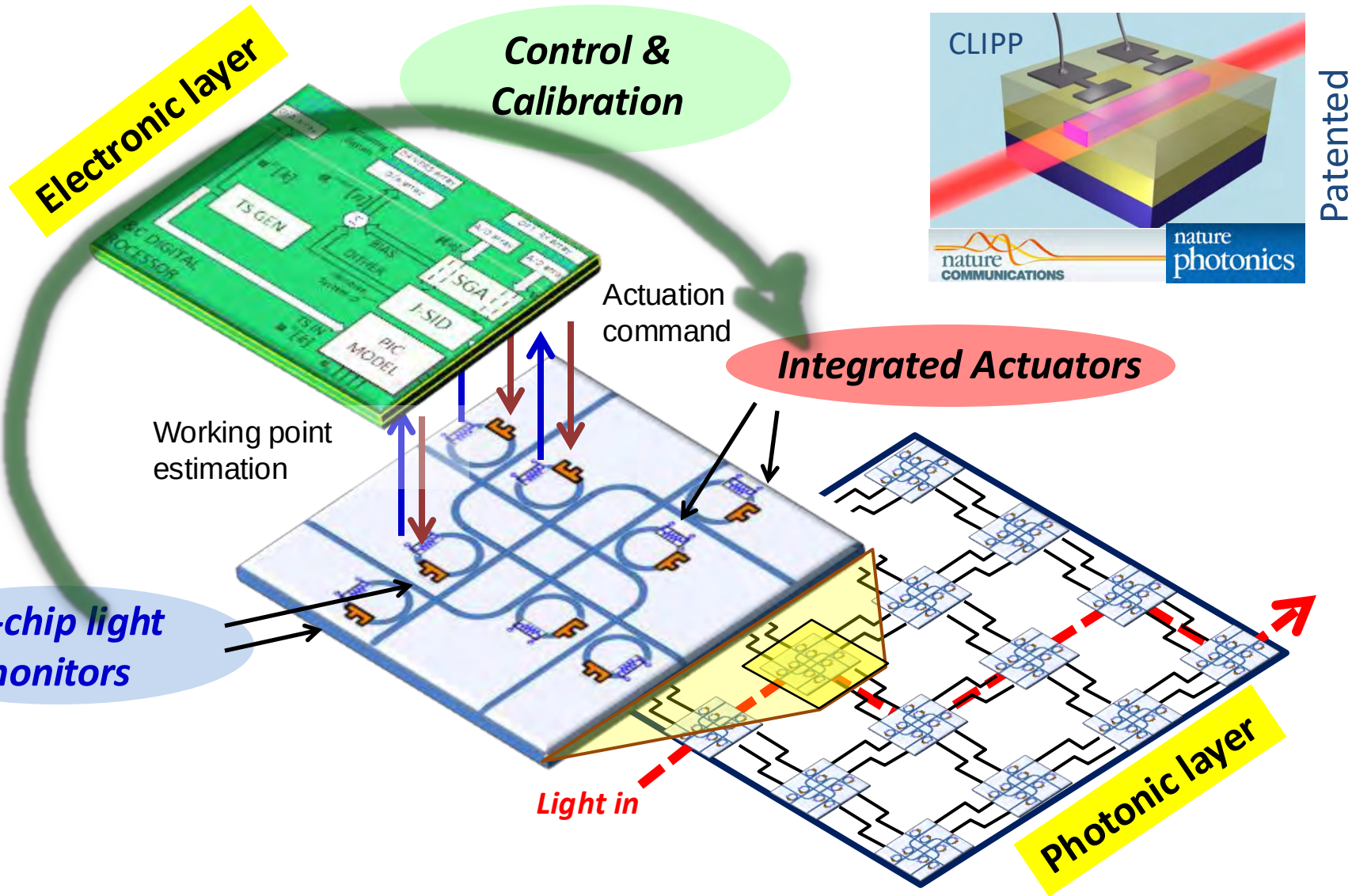


A microscopic image of a device, likely a superconducting circuit, featuring several glowing red loops and lines on a dark background. The loops are interconnected, forming a complex network. The text is overlaid on this image.

Toward a system...

***Monitor
(Phase) Actuators
Feedback and control***

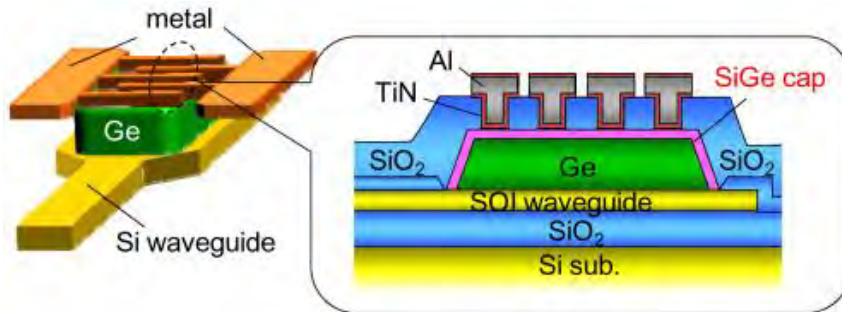
Control layer for photonic integrated circuits



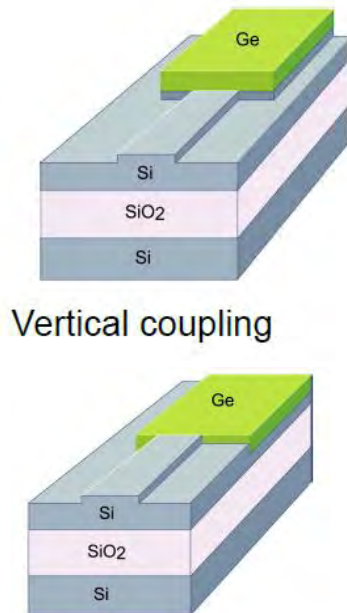
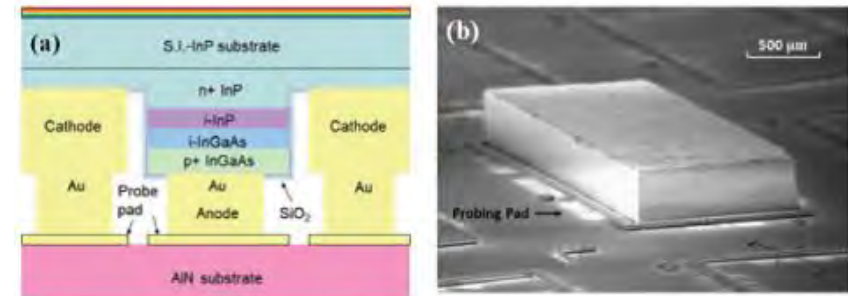
Light monitors: Ge, InP, hybrid, monolithic...



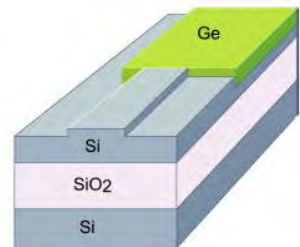
Ge on Silicon



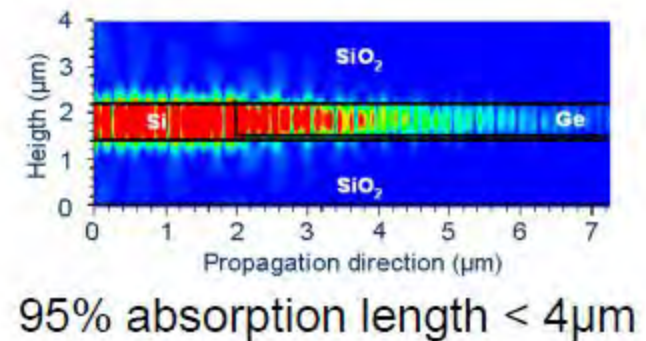
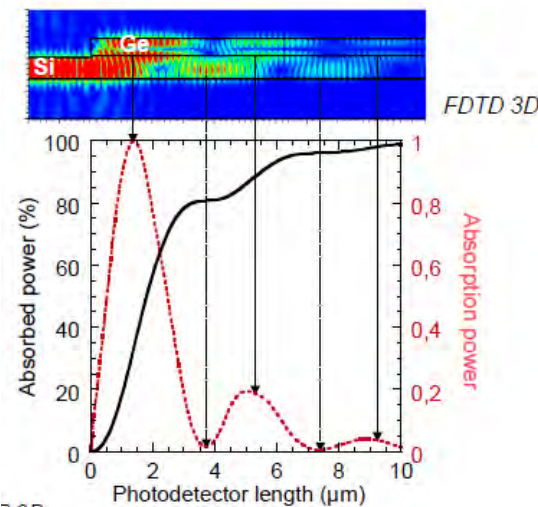
III-V compounds



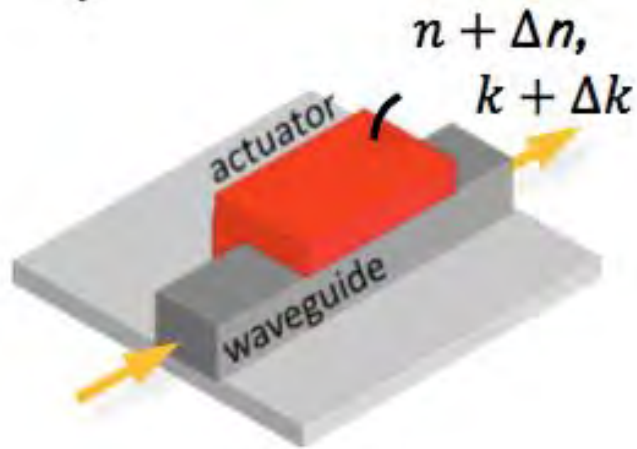
Vertical coupling



Butt coupling



- 4.2% Ge-Si Lattice mismatch
- ⇒ specific growth strategies required
- ⇒ growth on thin SiGe buffers
- ⇒ multi step growth process
- ⇒ thermal annealing (reduce dislocation density)



Phase / Amplitude

Fast (MHz for tuning and reconfiguration)

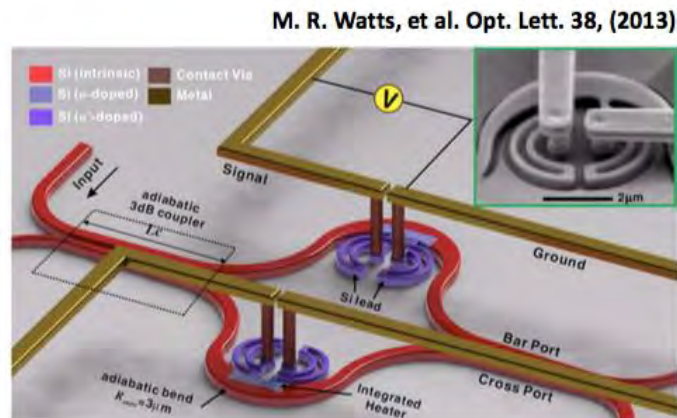
Compact (10-100 μm)

Low Power consumption (< mW)

Permanent, self holding to avoid to continuous feed

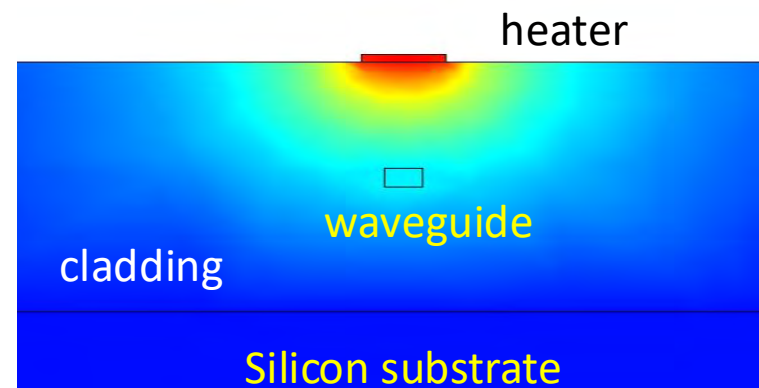
Analog / Digital

Thermal actuators, mature technology, power hungry



Si channel waveguide with embedded Si heater (n-doped)

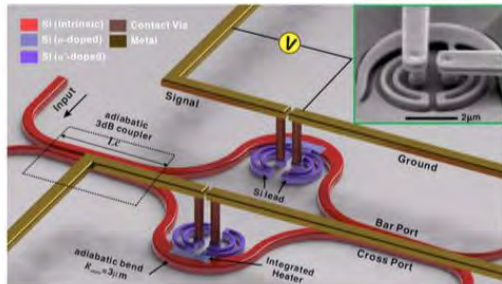
Thermal field induced by heater





Thermal actuators

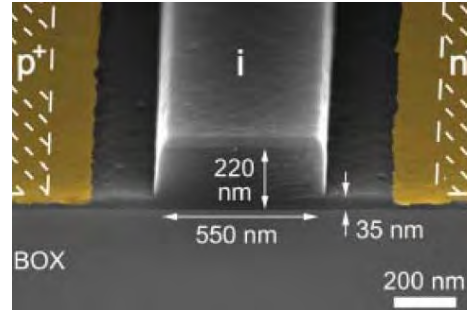
M. R. Watts, et al. *Opt. Lett.* 38, (2013)



Si channel waveguide with embedded Si heater (n-doped)

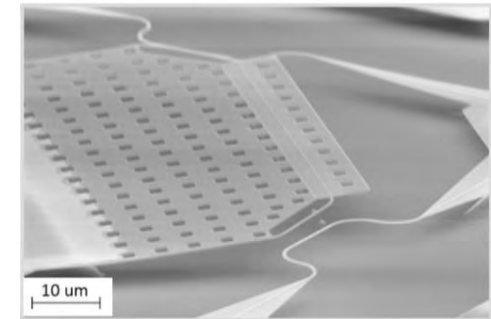
p-n junctions

Carrier injection/depletion



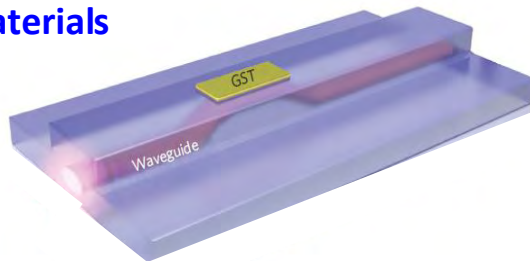
W.M. Green *et al.*, *Opt. Express* 15 (2007)

MEMS based switches



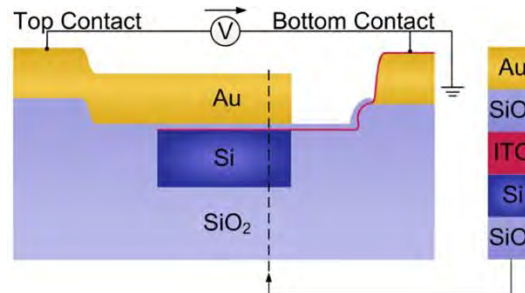
S. Han *et al.*, Berkeley, (2015)

Phase-change materials



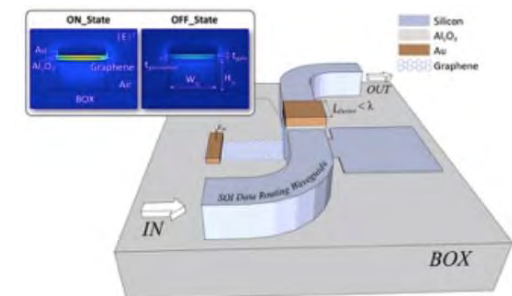
C. Rões *et al.*, *Nature Photonics* 6 (2015)
A. Joushaghani *et al.*, *APL*, 102, 061101 (2013)

Plasmonic memristor



C. Hoessbacher *et al.*, *Optica* 1 (2014)

Graphene, MoTe₂, ITO modulators

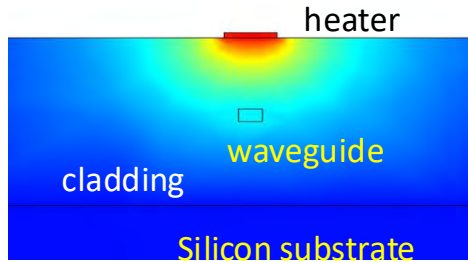


R. Amin *et al.*, arxiv (2018)

Integrated optical **actuators**

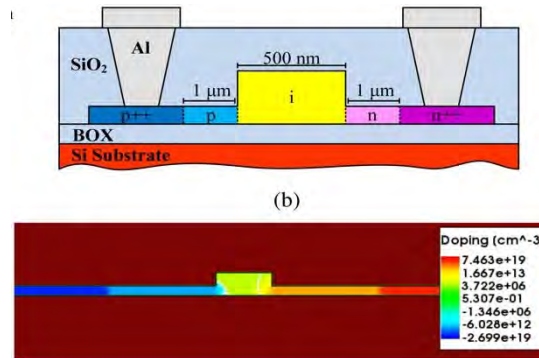


Thermal field induced by heater

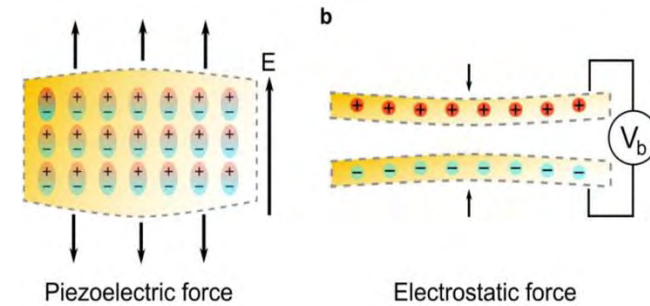


p-n junctions

Carrier injection/depletion



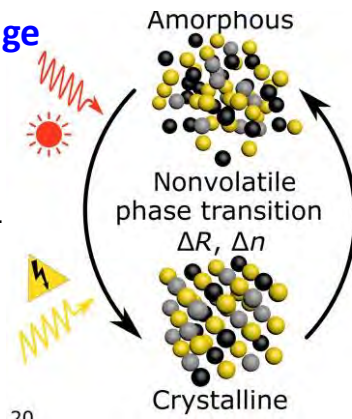
MEMS based switches



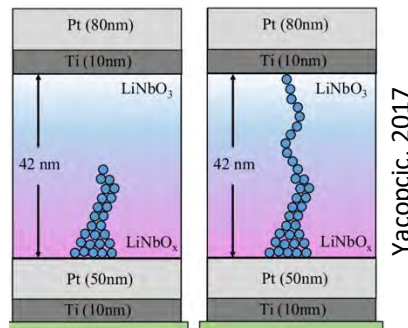
A. Fiore, TU/e

Phase-change materials

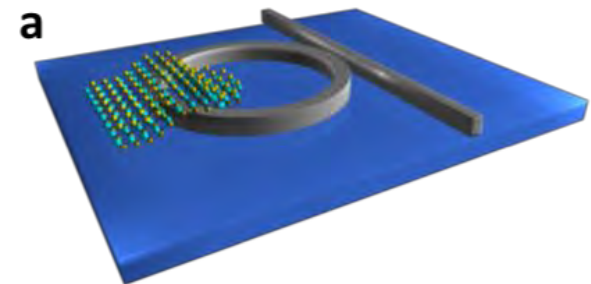
N. Farmakidis et al.
Sci Adv 2019; 5



Plasmonic memristor

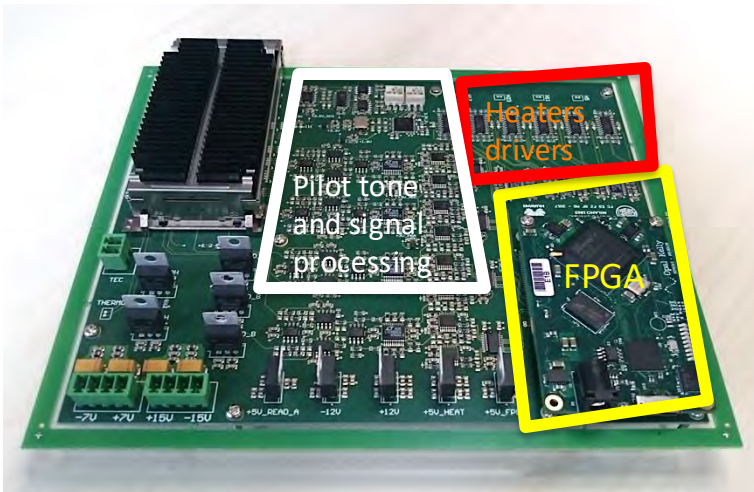
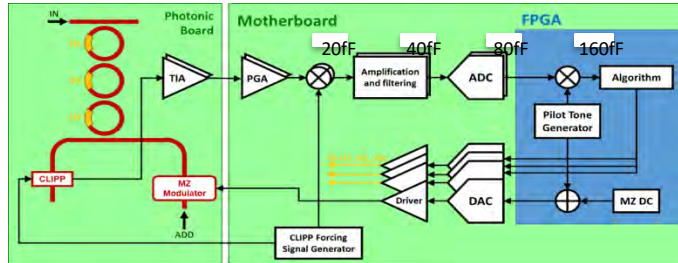


Graphene, MoTe₂, ITO modulators

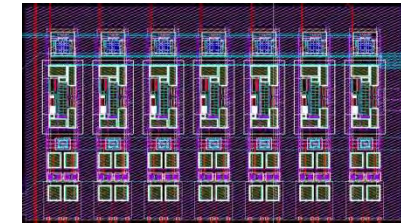
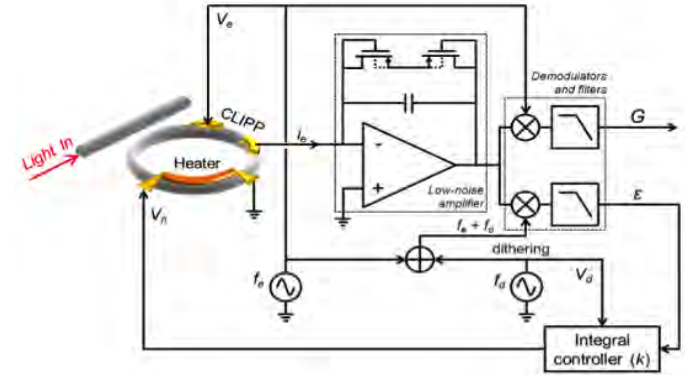




BRAIN – Central Control Unit

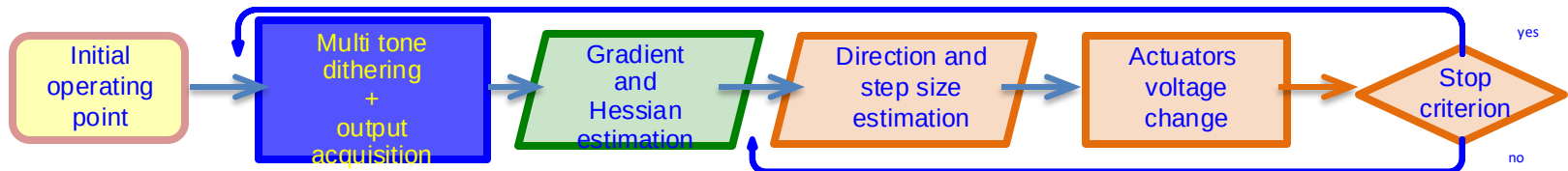


REFLEX ARC – Local Analog Control



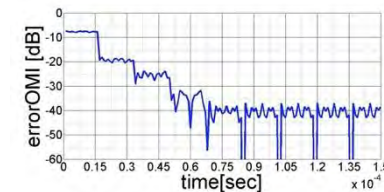
STm BCD8sp ASIC

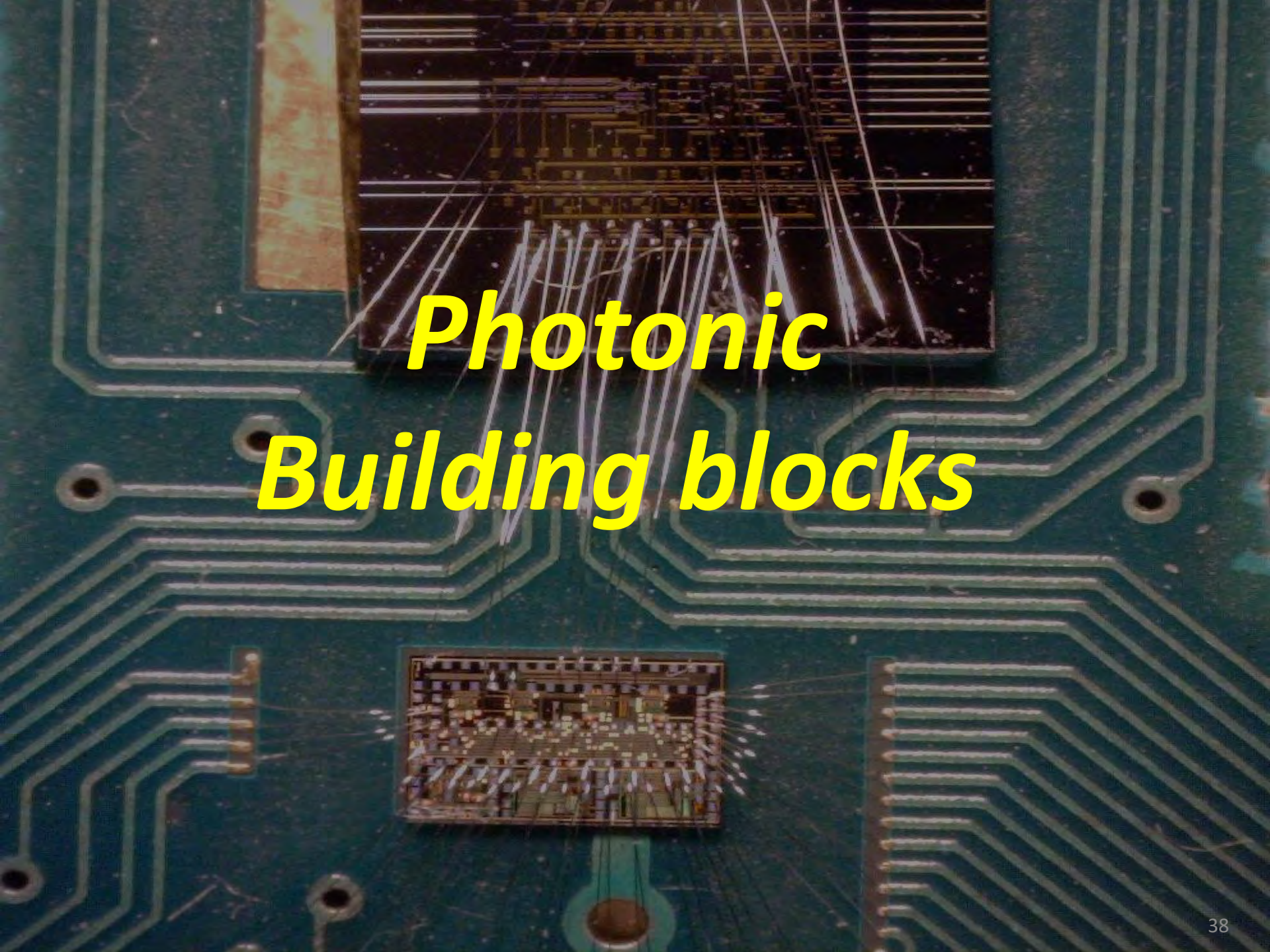
M-DOF



Control **many degrees-of-freedom** (DOFs) using a **single monitoring point**

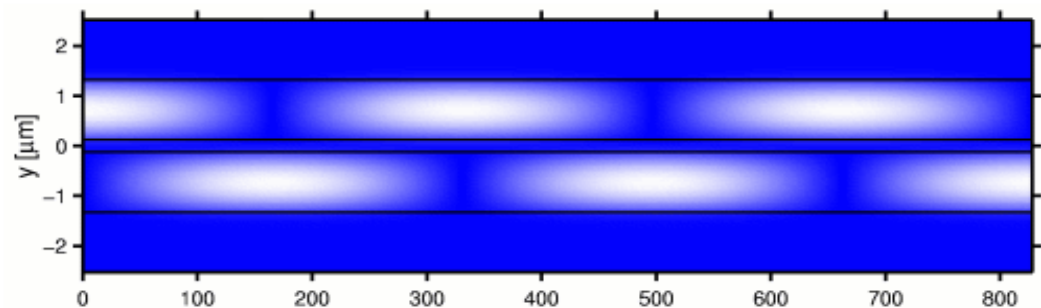
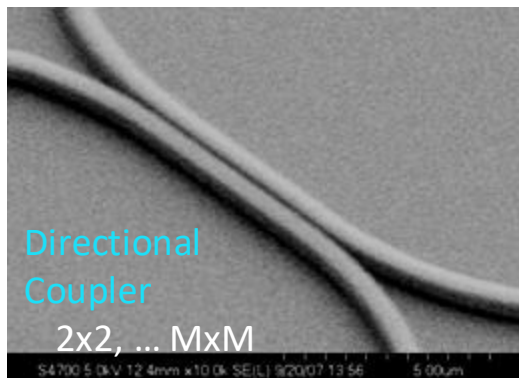
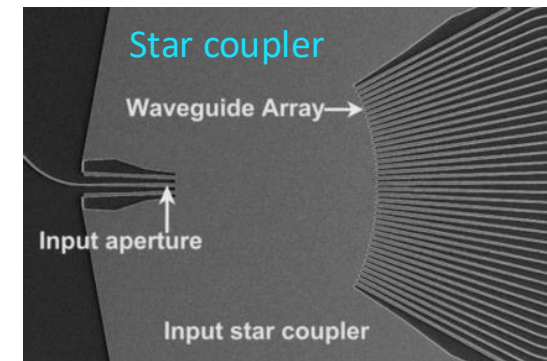
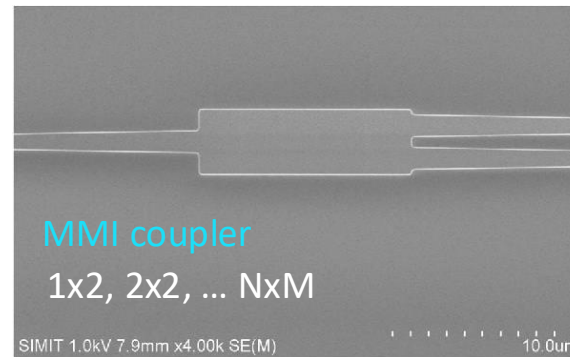
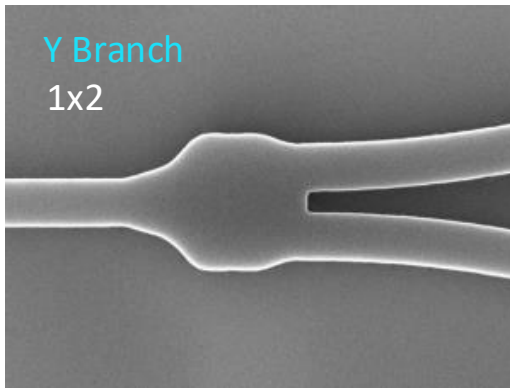
Several DOFs **simultaneously dithered at orthogonal frequencies** generated from a discrete-multi-tone generator





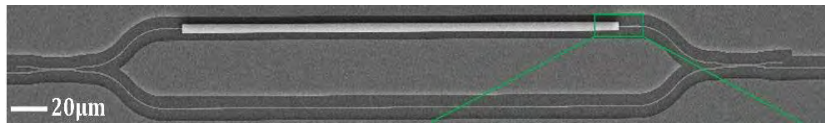
Photonic Building blocks

Integrated power splitters

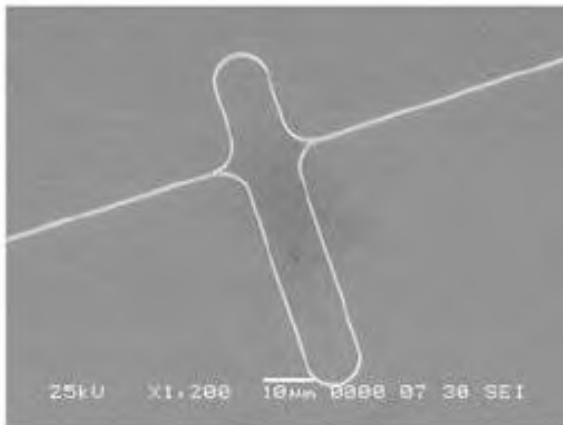


$$T_C = \begin{bmatrix} \cos(\kappa L) & -j \sin(\kappa L) \\ -j \sin(\kappa L) & \cos(\kappa L) \end{bmatrix} = \begin{bmatrix} r & -it \\ -jt & r \end{bmatrix}$$

Mach Zehnder interferometer (MZI)

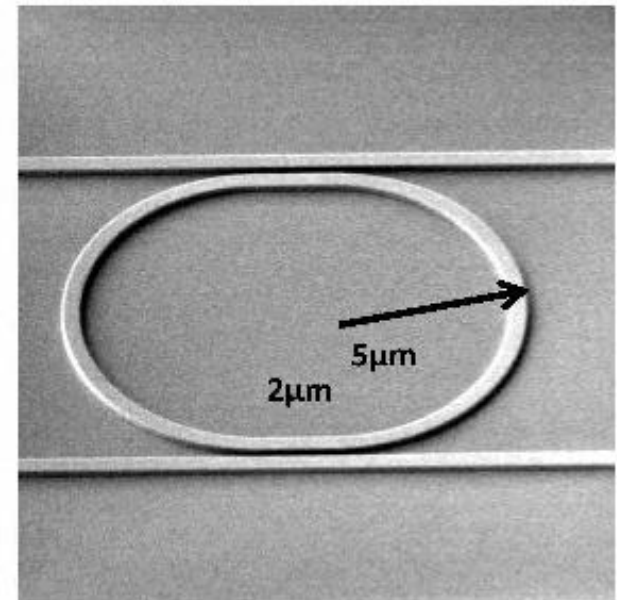


balanced



unbalanced

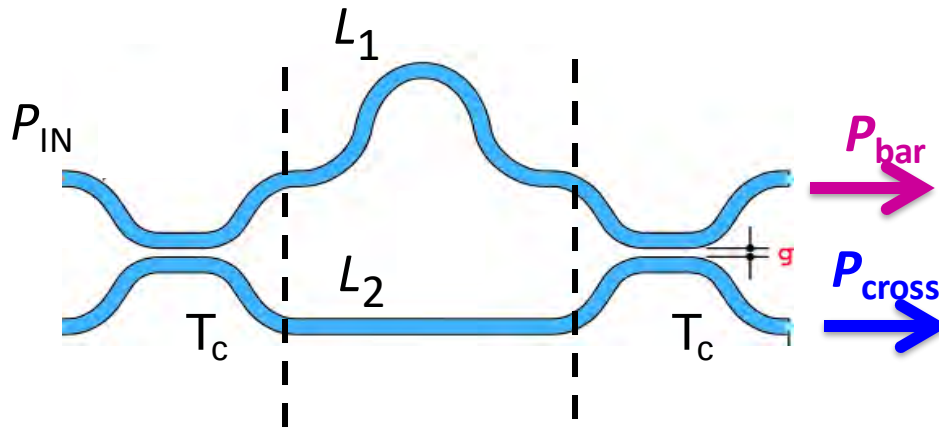
Microring resonator (MRR)



Mach-Zehnder interferometer (unbalanced)



feed-forward interferometer



MZI with 3 dB power splitter

$$\Delta L = L_1 - L_2$$

Geometric unbalance

$$\Delta\varphi_L = \frac{2\pi}{\lambda} n_{eff} \Delta L$$

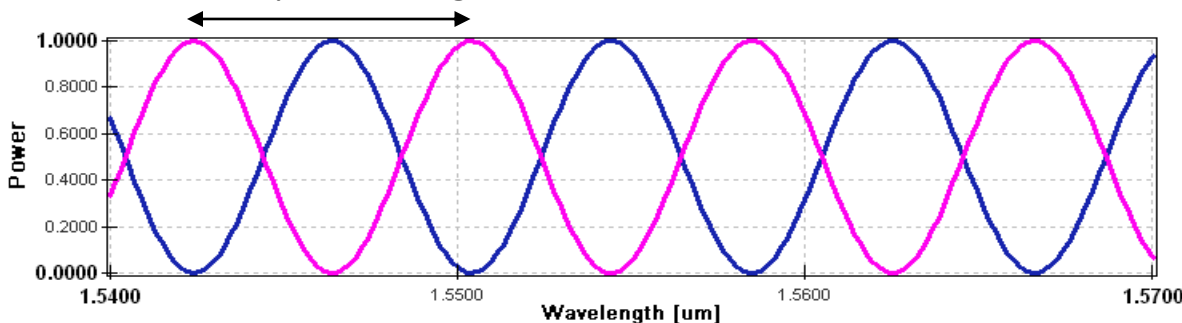
Phase unbalance

$$P_{bar} = \sin^2\left(\frac{\Delta\varphi_L}{2}\right) P_{IN}$$

$$P_{cross} = \cos^2\left(\frac{\Delta\varphi_L}{2}\right) P_{IN}$$

$$FSR = \frac{c}{n_g \Delta L}$$

Free spectral range (FSR)



n_g group index

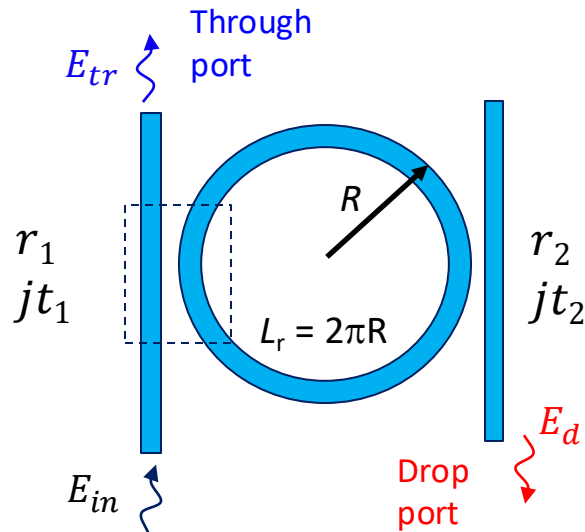
(takes into account chromatic dispersion)

$$n_g = \frac{c}{v_g} = \frac{c}{d\omega/d\beta} = n_{eff}(\omega) + \omega \frac{dn_{eff}}{d\omega}$$

Ring Resonator Filter



feed-back interferometer



$$H_{tr}(f) = \frac{E_{tr}}{E_{in}} = \frac{r_1 - r_2 e^{-\gamma L_r/2}}{1 - r_1 r_2 e^{-\gamma L_r}}$$

$$H_d(f) = \frac{E_d}{E_{in}} = \frac{t_1 t_2 e^{-\gamma L_r/2}}{1 - r_1 r_2 e^{-\gamma L_r}}$$

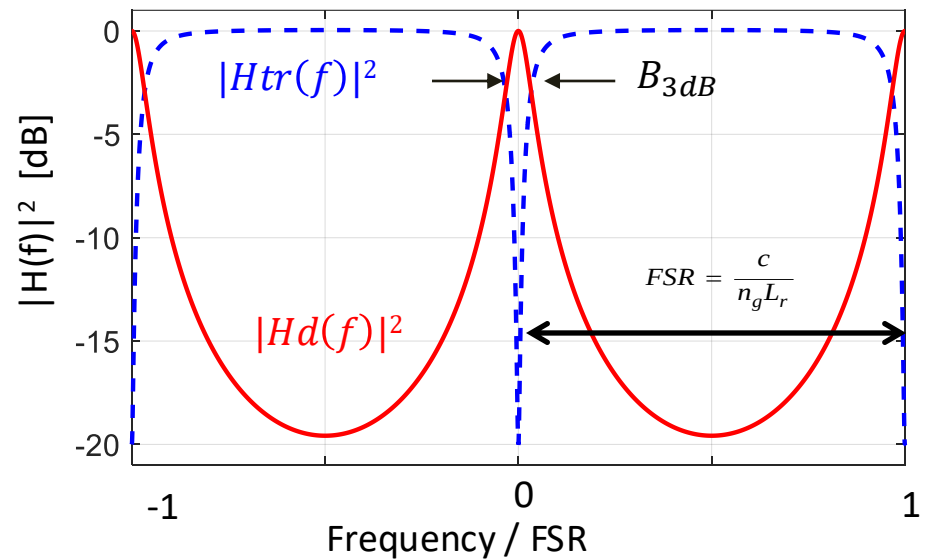
$\gamma = \alpha + j\beta$ Propagation constant

$\beta = \frac{\omega}{c} n_{eff}$ Phase constant

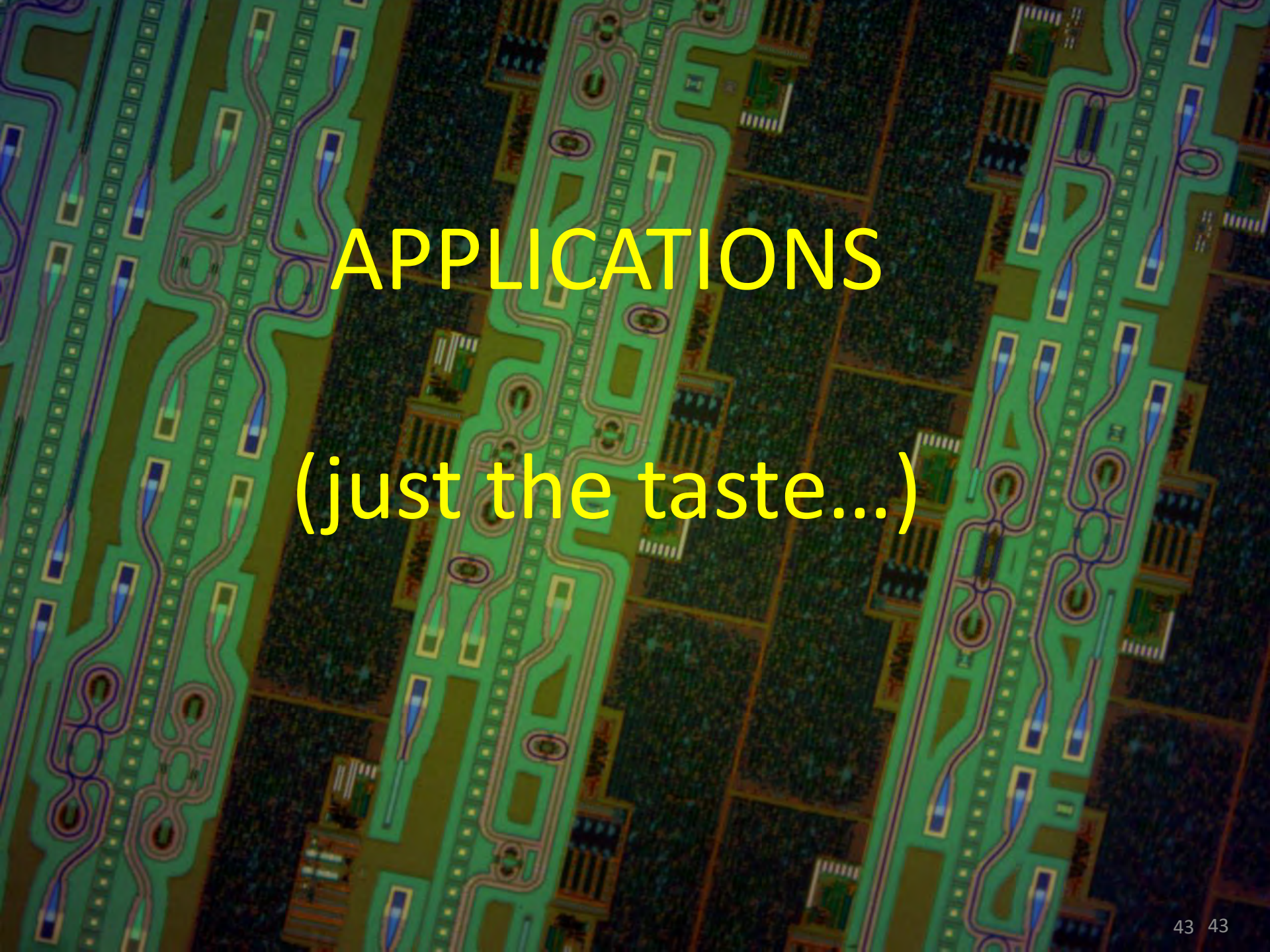
α Attenuation constant

- Same frequency resonance as a Fabry-Pérot cavity
- Lossless case ($\alpha = 0$), $|H_{tr}(f_0)|^2 = 0$ if $r_1 = r_2$
- Lossless ($\alpha = 0$) & symmetric ($r_1 = r_2 = r$)

$$B_{3dB} \cong FSR \frac{t^2}{\pi}$$



$$\beta L_r = M 2\pi \rightarrow f_{0,M} = \frac{c}{L_r n_{eff}} M \quad \text{resonance frequencies}$$

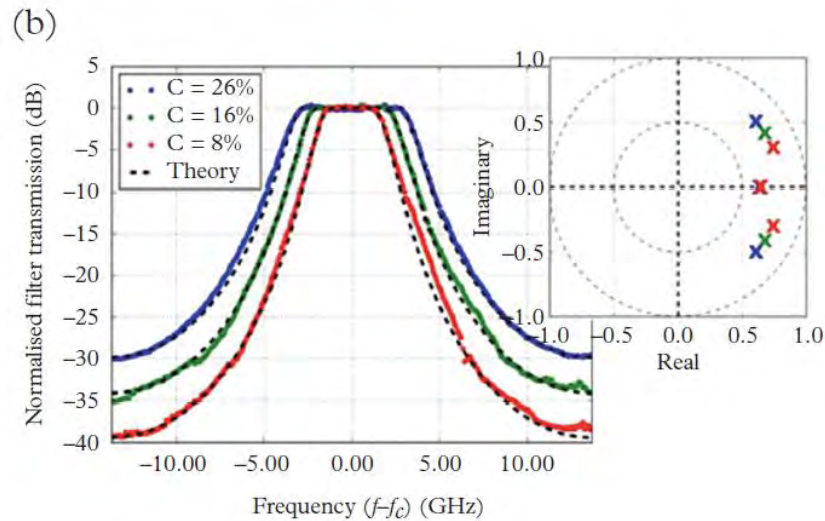
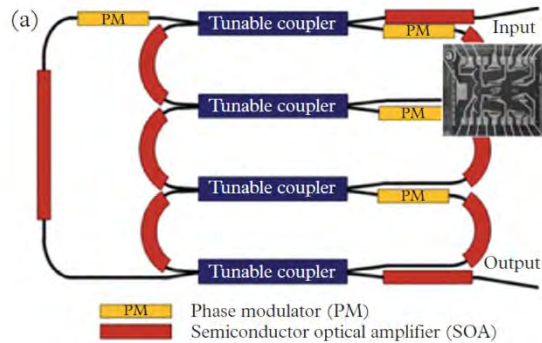
An aerial photograph of a city grid, likely New York City, with a green overlay indicating a network of paths or routes. The paths are shown in green and purple, winding through the city blocks. The text "APPLICATIONS (just the taste...)" is overlaid in yellow.

APPLICATIONS

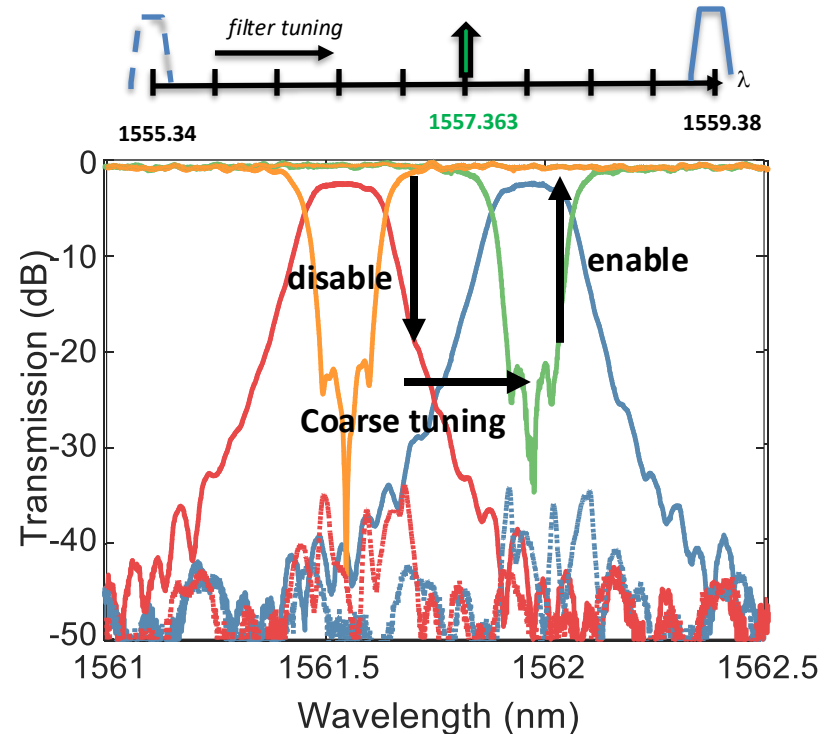
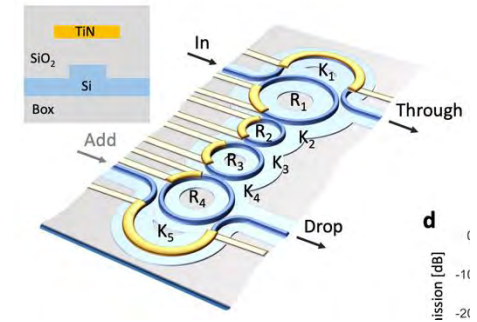
(just the taste...)

Reconfigurable filters

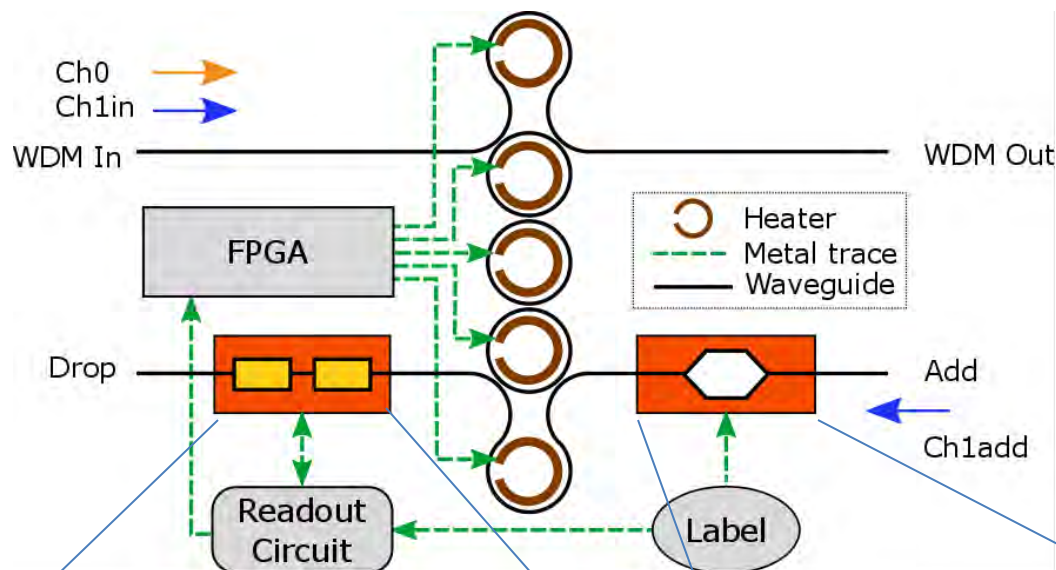
Tunable bandwidth filter



Reconfigurable hitless filters



Reconfigurable hitless filter

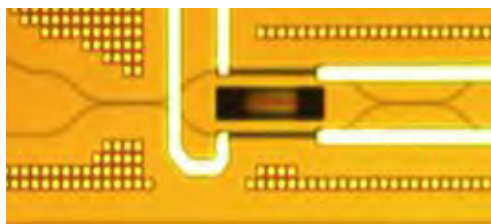


Filter characteristics:

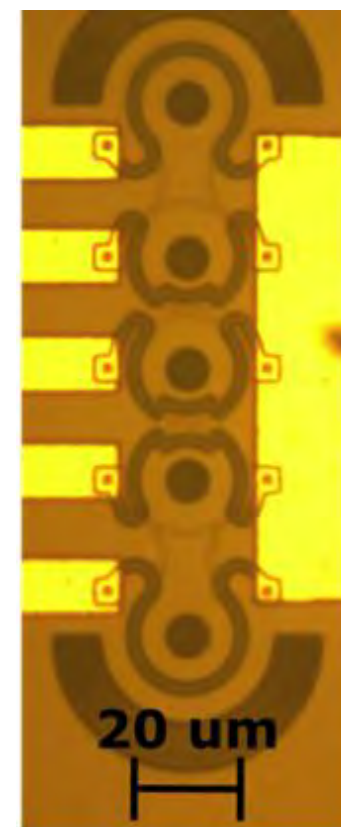
- Hitless tuning
- 1 THz (8 nm) of Free Spectral Range (FSR)
- 40 GHz of 3 dB bandwidth
- 20 dB in band isolation

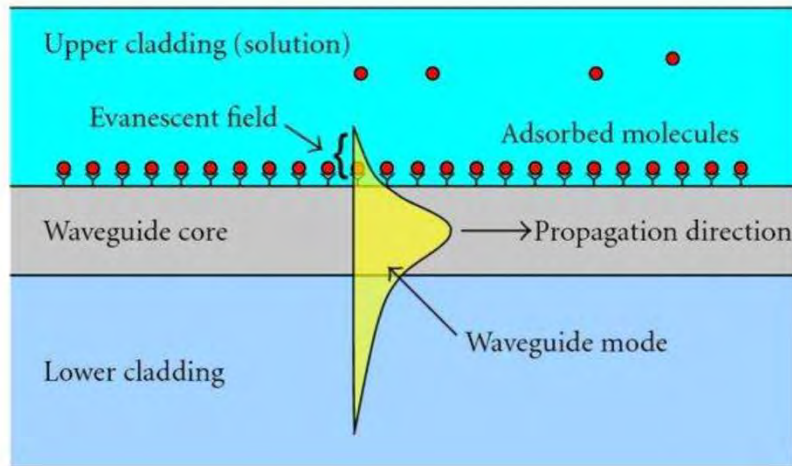


CLIPP at the Drop port to read optical label

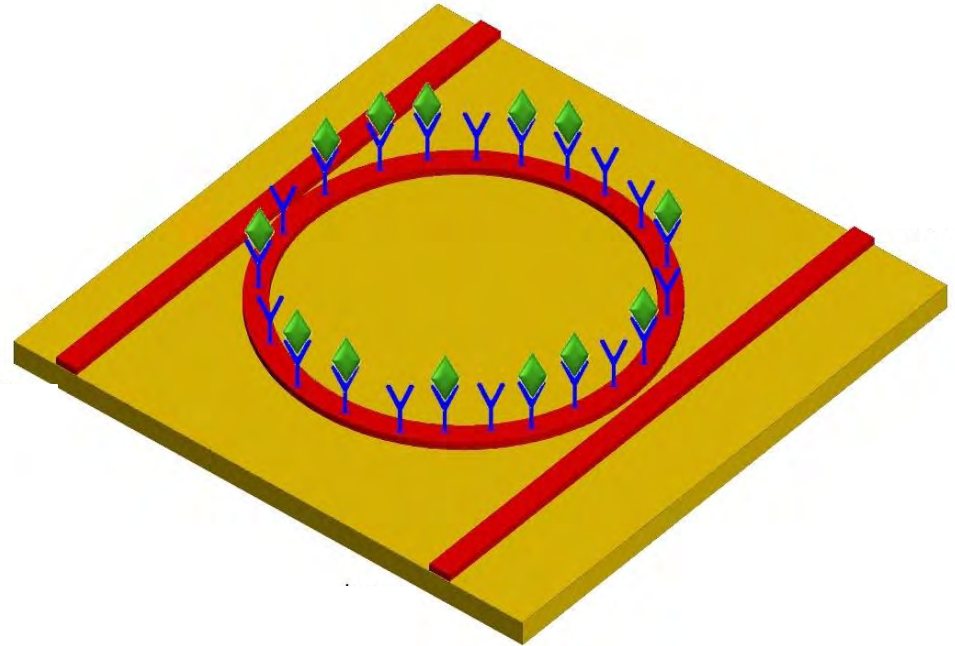


Mach-Zehnder Modulators (MZM) in the add port to apply optical label



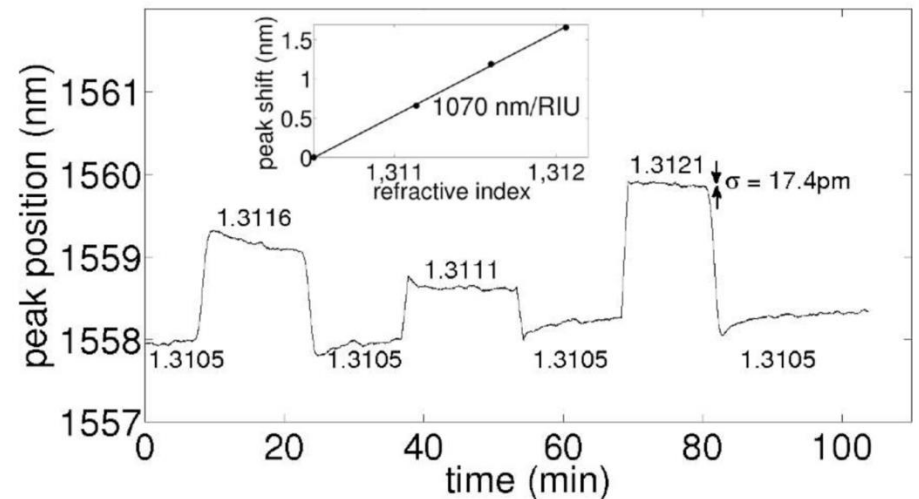
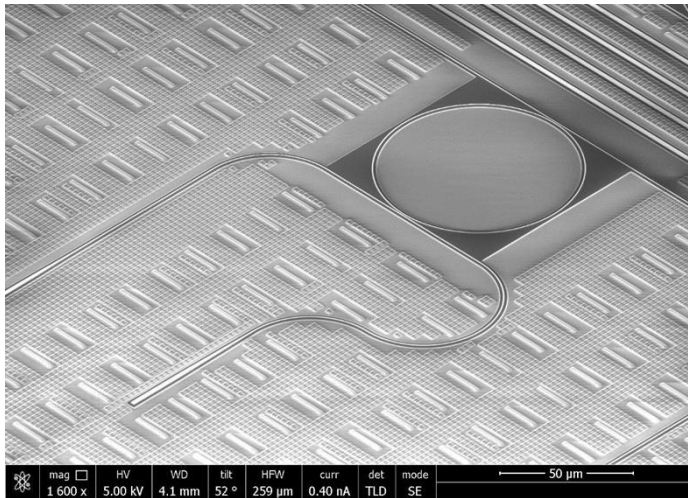
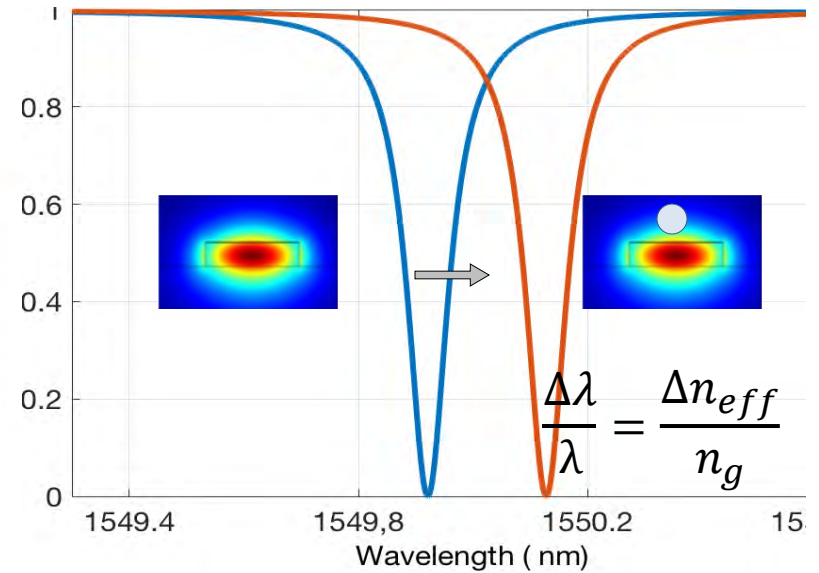
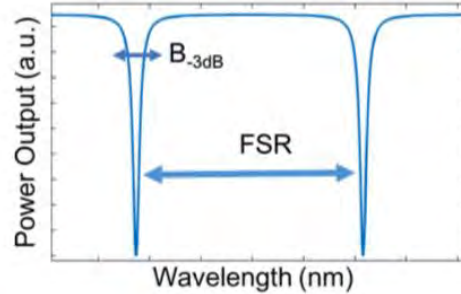
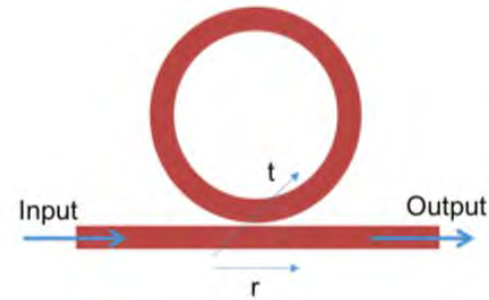


Evanescent field detection
Negligible absorption
Phase change of the light



Phase-intensity conversion with an
“interferometer” (ring resonator)

Biosensing and integrated photonics





Photonic Computing

Forbes

FORBES > INNOVATION

Optical Computing: What It Is, And Why It Matters

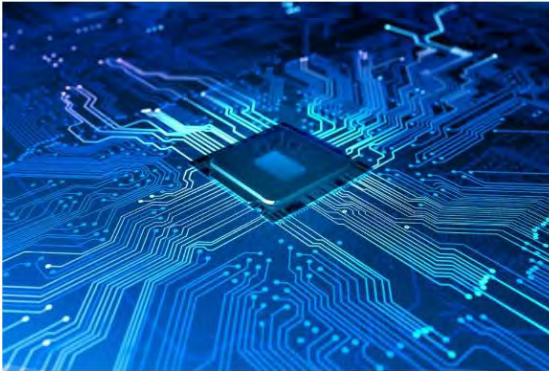


Kazuhiro Gomi Forbes Councils Member
Forbes Technology Council COUNCIL POST | Membership (Fee-Based)



Sep 10, 2024, 09:30am EDT

Kazuhiro Gomi, NTT Research CEO. Leads research in physics & informatics, cryptography & information security, medical & health informatics.

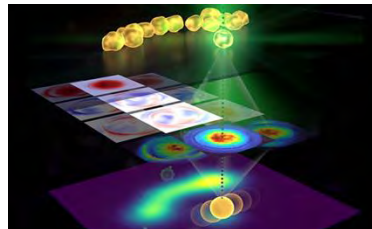


<https://www.forbes.com/councils/forbestechcouncil/2024/09/10/optical-computing-what-it-is-and-why-it-matters/>

Positioning & Ranging (LIDAR)



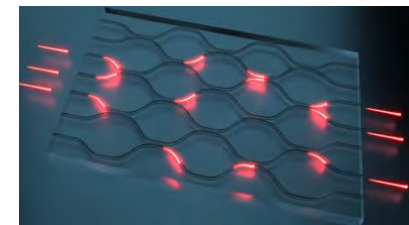
Beam forming, imaging & microscopy



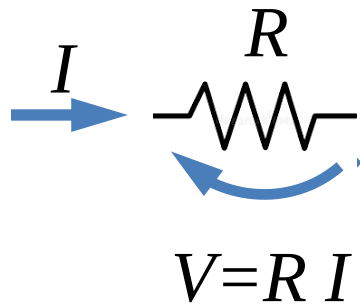
Micro-projectors & augmented reality



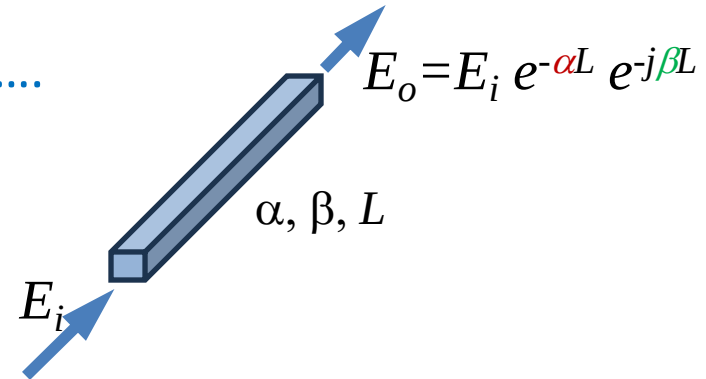
Quantum photonics (communication, computing & sensing)



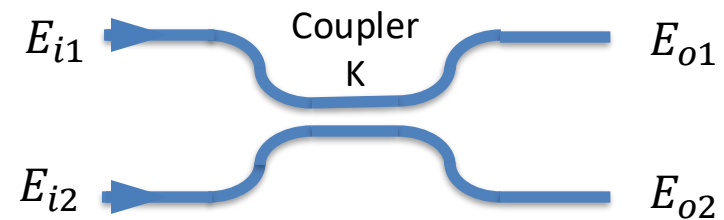
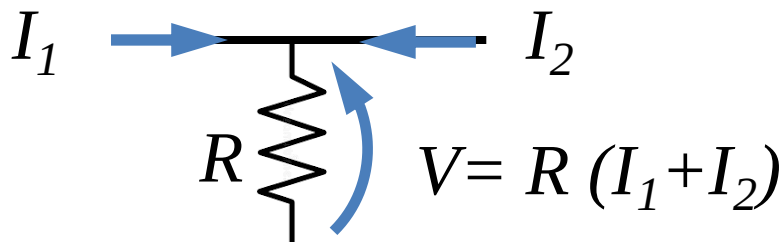
- **Electronic computing...** two decades ago, GPUs were starting to supplant CPUs
- **Moore's law** is fading
- The **von Neumann** computing model (memory separated from processing since the 1940s) has inherent limits
- To address big computing challenges, it helps to think big and in new ways...
- Use photons instead of electrons... (somewhere)
- A general-purpose **optical neural network** may be years out... but could end up being **1,000 times as efficient as its electronic counterparts**



Multiplication



Sum



$$E_{o1} = \sqrt{1-K} E_1 + j \sqrt{K} E_2$$

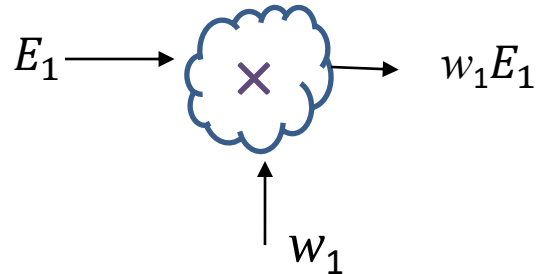
... è una **interferenza** (→ **sommatore coerente**)

Multiplication by a complex weight



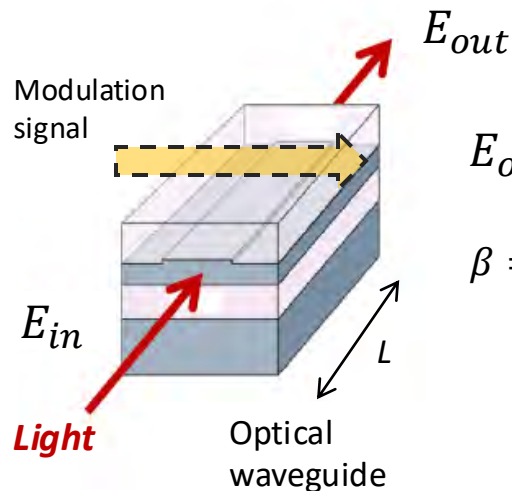
Let's consider an optical signals (frequency, polarization and spatial mode here is not much relevant) with power P_1

$$P_1 \propto |E_1|^2$$



... basically it is an **amplitude & phase** modulation

$$w_1 = e^{-\alpha L} e^{-j\beta L}$$



$$E_{out} = E_{in} e^{-\alpha L} e^{-j\beta L}$$

$$\beta = \frac{2\pi f_0}{c} n_{eff}$$

Electro-absorption

Change of the attenuation constant (α) by an external applied signal

Intensity modulation

$$|w_1| = e^{-\alpha L}$$

Electro-refraction & Thermal

Change of the refractive index (phase constant β) by an external applied signal

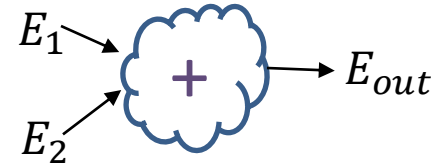
Phase modulation

$$\angle w_1 = -\beta L$$

Summing... amplitude or power?



Let's consider 2 optical signals (same frequency, polarization and spatial mode)
with power P_1 and P_2 respectively



Is it possible to get the signal “sum” with field amplitude $E_{out} = E_1 + E_2$?

Can we implement a field «amplitude adder»? **NO !!!**

A simple justification

$$P_1 \propto |E_1|^2$$

$$E_1 = 1 \quad P_1 = 1$$

$$P_2 \propto |E_2|^2$$

$$E_2 = 1 \quad P_2 = 1$$

$$E_{out} = E_1 + E_2 = 1 + 1 = 2 \quad P_{out} = 4$$



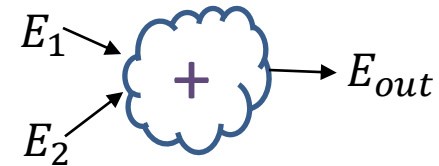
instead ... $P_{in} = P_1 + P_2 = 2$

There is no way to make an «electric field adder»
(... power conservation !)

A fundamental issue... the photonic power adder

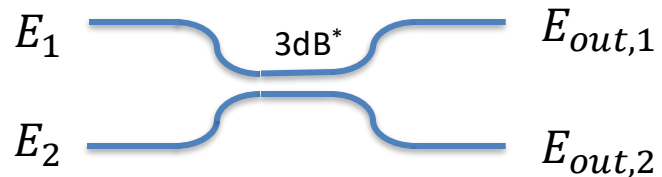


Let's consider 2 optical signals (same frequency, polarization and spatial mode) with power P_1 and P_2 respectively



How to get the signal “sum” with power $P_{out} = P_1 + P_2$?

Can we use a «power combiner»... like a directional coupler ?



$$T_c = \frac{1}{\sqrt{2}} \begin{bmatrix} 1 & -j \\ -j & 1 \end{bmatrix}$$

$$E_{out,1} = \frac{1}{\sqrt{2}} E_1 - j \frac{1}{\sqrt{2}} E_2$$

$$E_{out,2} = -j \frac{1}{\sqrt{2}} E_1 + \frac{1}{\sqrt{2}} E_2$$

$$P_{out,1} = P_1 + P_2$$

$$P_{out,2} = 0$$

... only if

$$|E_1| = |E_2| \longrightarrow P_1 = P_2$$

$$\angle E_1 - \angle E_2 = -\frac{\pi}{2}$$

The output power depends on the amplitude and the phase of the input signals !(*)

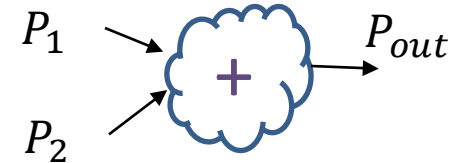
... that's **interference** (→ **coherent adder**)

(*) using non-3dB couplers, phase dependence will remain anyway !

Non-coherent adder (= summing orthogonal signals)



If we want the output power NOT depend on the **amplitude** and the **phase** of the input signals...
... we need to avoid **interference**

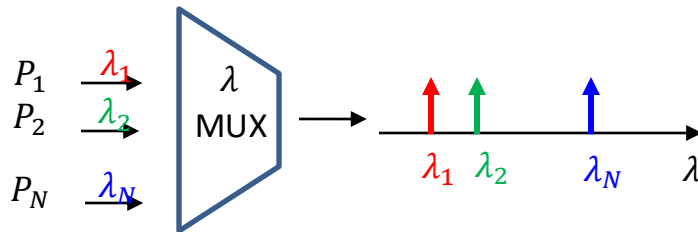
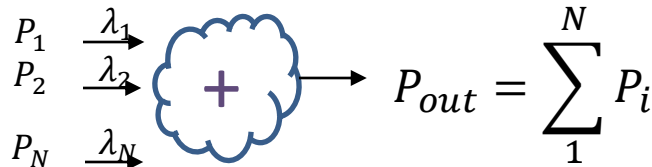


Interference may happen only if signals share frequency, polarization and spatial mode)

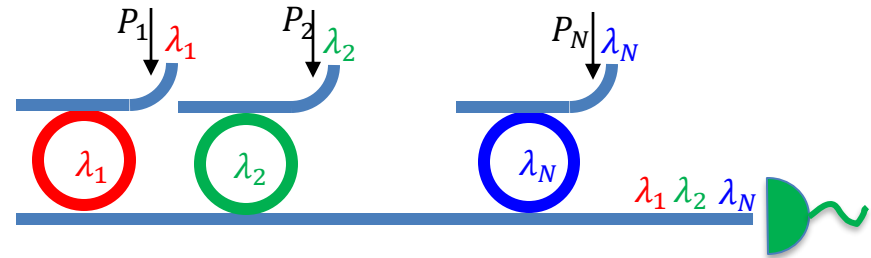
Use different frequencies/wavelengths (non-coherent adder)

$$P_1 \propto |E_1|^2$$

$$P_2 \propto |E_2|^2$$



An example of implementation



Different frequencies mean that the signals are **orthogonal** in the frequency domain

$$I_{out} \sim P_{out} = |E_1 \cos(\omega_1 t) + E_2 \cos(\omega_2 t)|^2 = |E_1|^2 + |E_2|^2 + \dots \cos(\omega_1 - \omega_2) + \dots \cos(\omega_1 + \omega_2)$$



$$Y = WX = \begin{bmatrix} w_{11} & w_{12} & \dots & w_{1N} \\ w_{21} & w_{22} & \dots & w_{2N} \\ \dots & \dots & \dots & \dots \\ w_{N1} & w_{N2} & \dots & w_{NN} \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ \dots \\ x_N \end{bmatrix}$$

The photonic circuit implement a NxM linear transformations **W** (matrix)

Matrix–vector multiplication (MVM) is one of the fundamental mathematical operations widely used in data “processing”:

- convolution, factorization, linear equalization, filtering
- Fourier transform (and other linear transforms e.g., Hadamard, Gram-Schmidt, etc.)
- Neural networks (weighted interconnections between adjacent neurons)

$$y_n = \sum_{m=1}^M w_{n,m} x_m$$

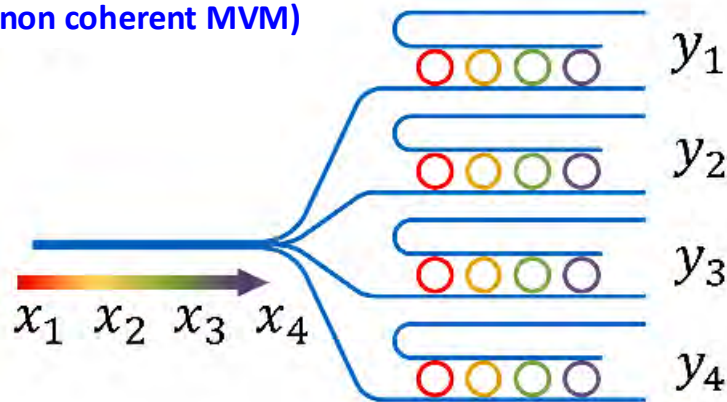
It basically translates in doing **multiplications** of optical signals (x_i) with **weights** (w_{ij}) and **sums** them up

How to implement it optically?



$$Y = WX = \begin{bmatrix} w_{11} & w_{12} & \dots & w_{1N} \\ w_{21} & w_{22} & \dots & w_{2N} \\ \dots & \dots & \dots & \dots \\ w_{N1} & w_{N2} & \dots & w_{NN} \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ \dots \\ x_N \end{bmatrix} \quad y_n = \sum_{m=1}^M w_{n,m} x_m$$

Integrated optics
(non coherent MVM)

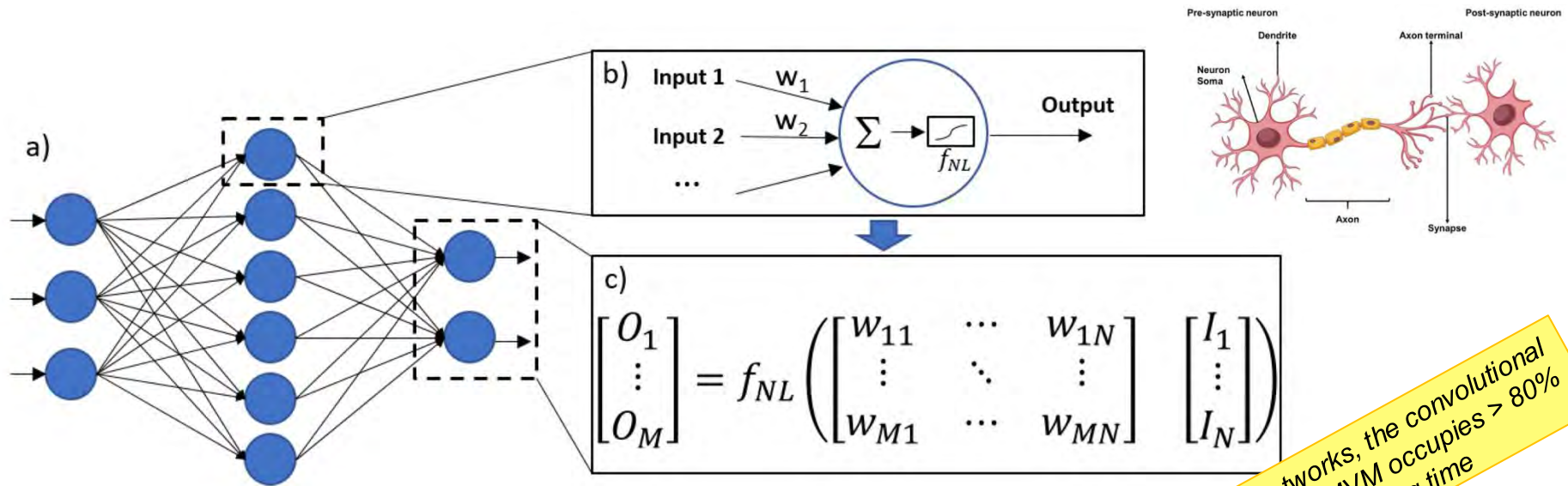


A filter bank is used to scale the various elements (**multipliers**)

PDs detect only the optical power (not the complex amplitude)

In non coherent MVM weights are **real numbers**

J. Cheng et al., «Photonic Matrix Computing: From Fundamentals to Applications», *Nanomaterials*, 11, 1683 (2021)



- A network with a large number of **interconnections** relative to logical nodes (e.g., the brain has 10^{11} neurons and 10^{15} synapses)

- **Distributed processing** based on weighted interconnections & localized nodes having **simple logic**

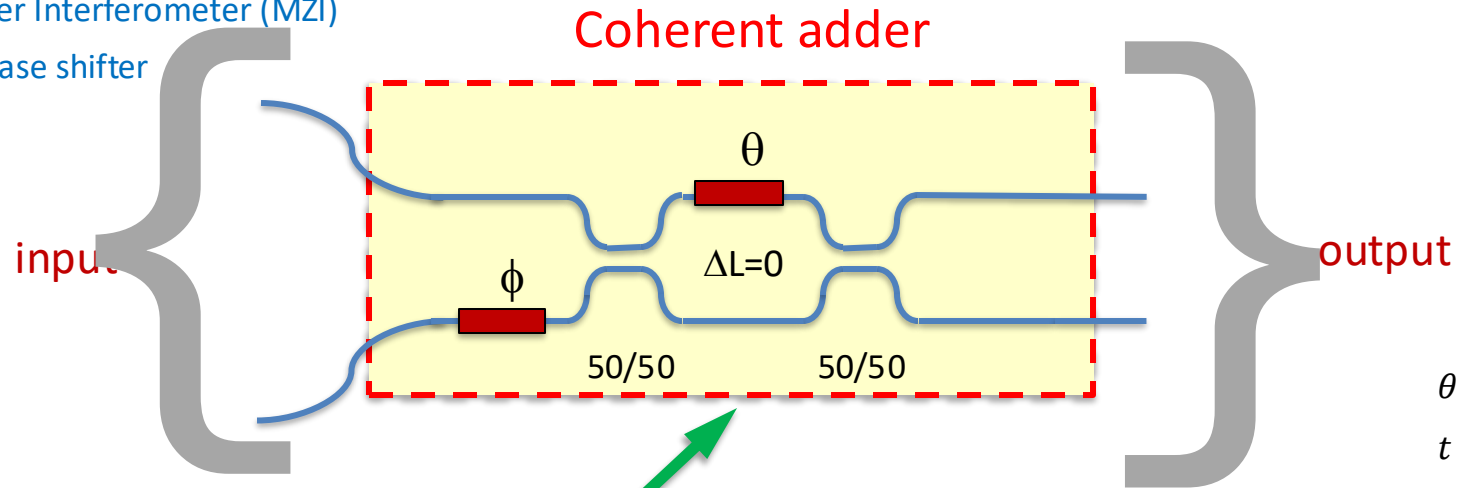
- **Nonlinearity** required to implemented decision making and model complex systems

In neural networks, the convolutional part based on MVM occupies > 80% of the total processing time

Coherent MVM: MZI is the simplest coherent combiner



Mach-Zehnder Interferometer (MZI)



$$\theta = 2\cos^{-1} r$$

$$t = \sqrt{1 - r^2}$$

$$U_2 = -je^{j\theta/2} \begin{bmatrix} \sin(\theta/2) & \cos(\theta/2) e^{j\phi} \\ \cos(\theta/2) & -\sin(\theta/2) e^{j\phi} \end{bmatrix} = -je^{j\theta/2} \begin{bmatrix} t & re^{j\phi} \\ r & -te^{j\phi} \end{bmatrix}$$

*2x2 Unitary
Transformation*

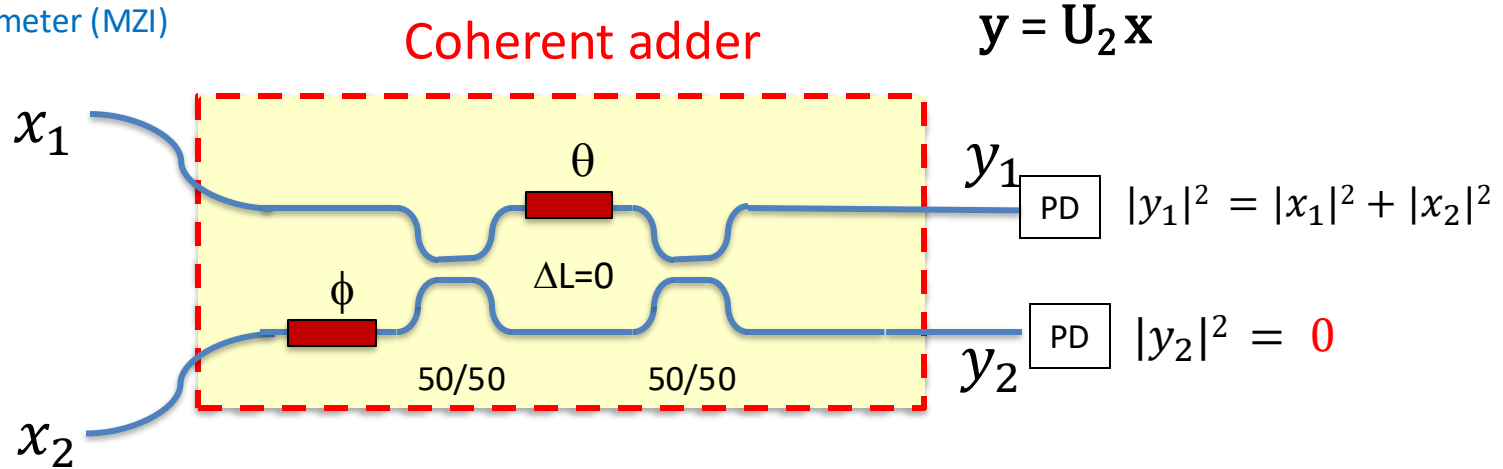
- $U^\dagger U = U U^\dagger = I$, $U^{-1} = U^\dagger$, $\det(U) = 1$
- preserves inner product $\langle Ux, Uy \rangle = \langle x, y \rangle$, i.e.,
- preserves “length” & “angle” (only a “rotation”) $\Rightarrow$ power conservation
- eigenvalues on unit circle, orthogonal eigenvectors



Mach-Zehnder Interferometer (MZI)

 Phase shifter

$$\mathbf{x} = \begin{bmatrix} x_1 \\ x_2 \end{bmatrix}$$



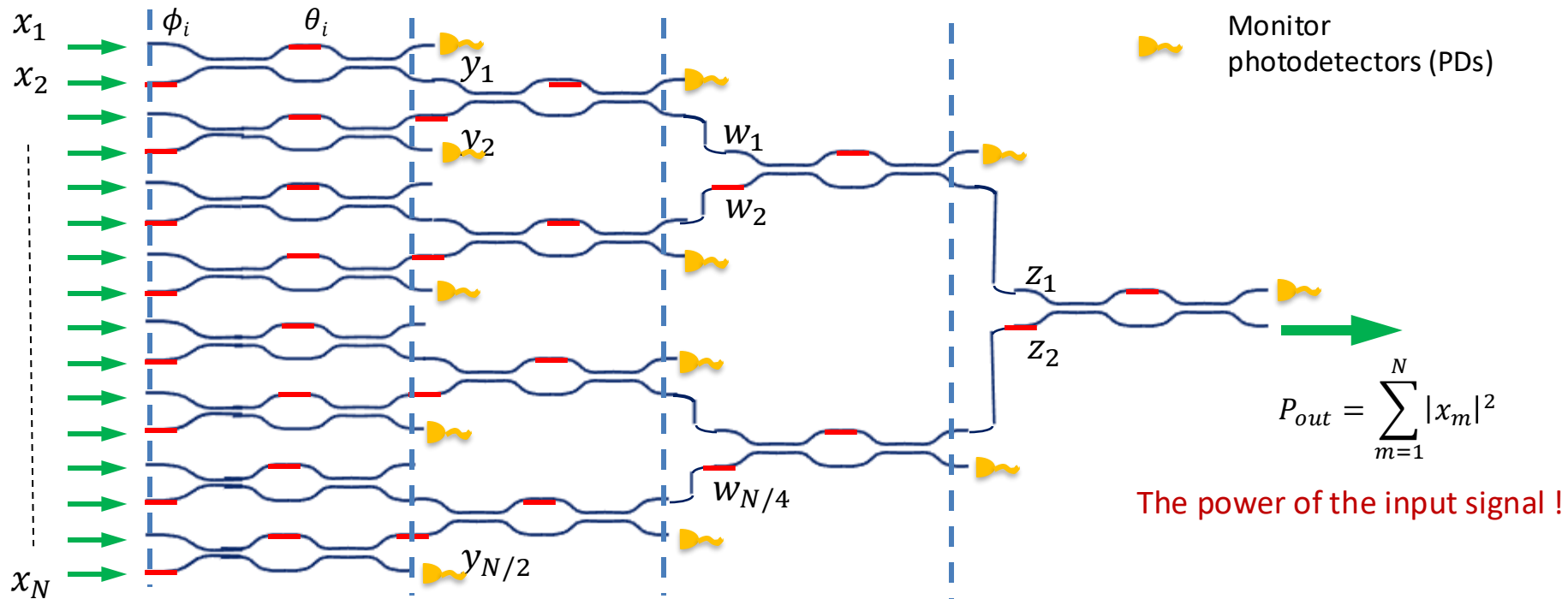
Condition to null the output power at port 2

$$y_2 = -je^{j\theta/2} \left[\cos\left(\frac{\theta}{2}\right) x_1 - e^{j\phi} \sin\left(\frac{\theta}{2}\right) x_2 \right] = 0$$

$$\Rightarrow \cos\left(\frac{\theta}{2}\right) x_1 = e^{j\phi} \sin\left(\frac{\theta}{2}\right) x_2$$

$$\Rightarrow \begin{cases} \theta = 2 \tan^{-1} \left| \frac{x_1}{x_2} \right|, & \theta \in [0, \pi] \\ \phi = (\angle x_1 - \angle x_2) + 2N\pi \end{cases}$$

Nx1 coherent adder - Binay tree MZI mesh

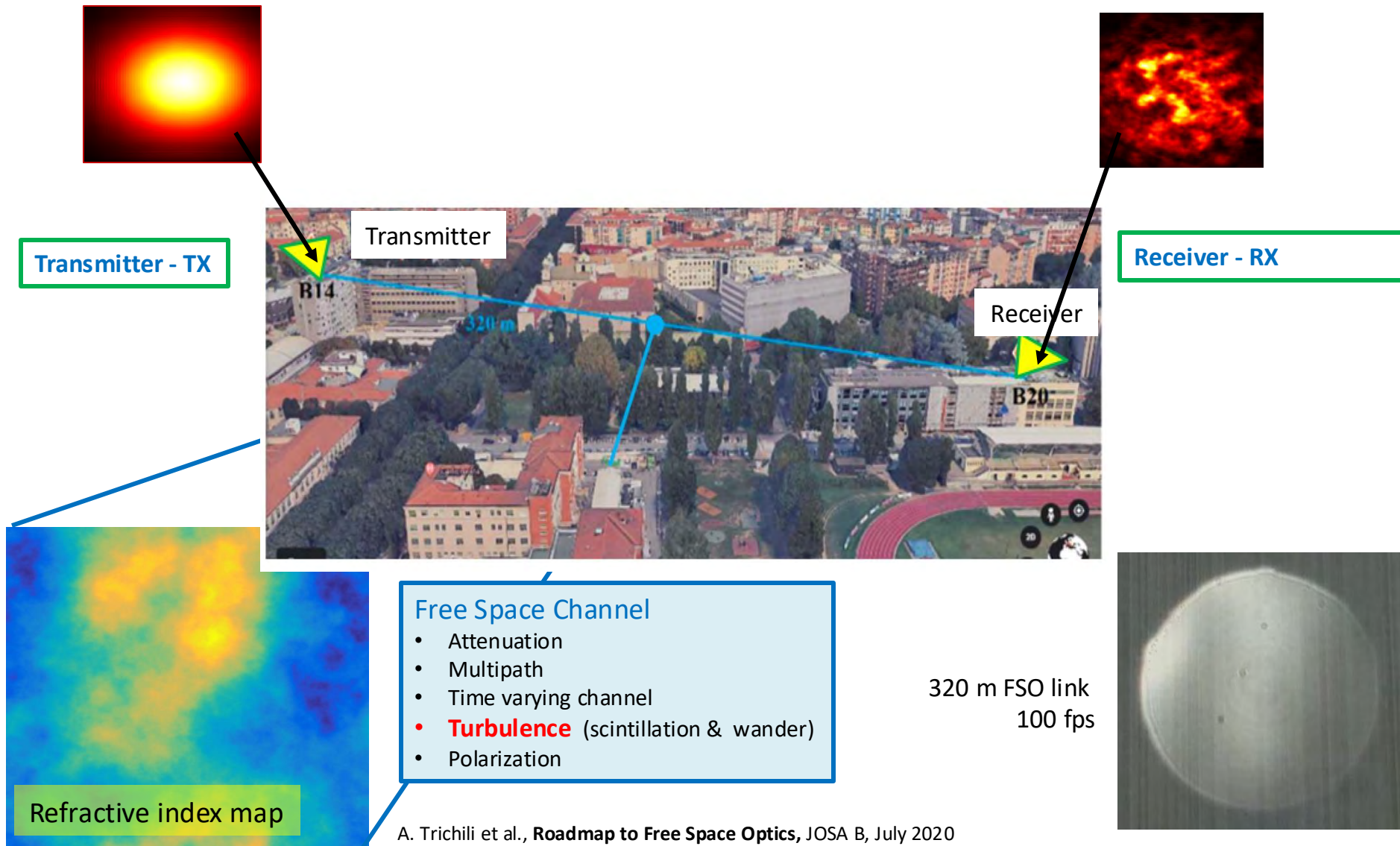


$$\phi_i = \angle x_{i+1} - \angle x_i$$

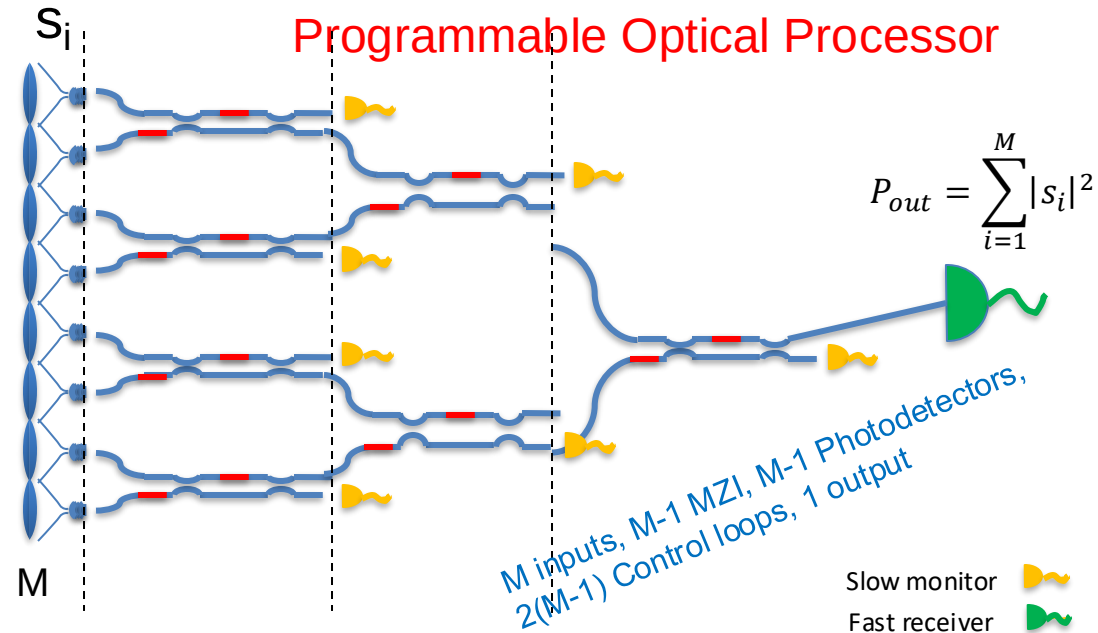
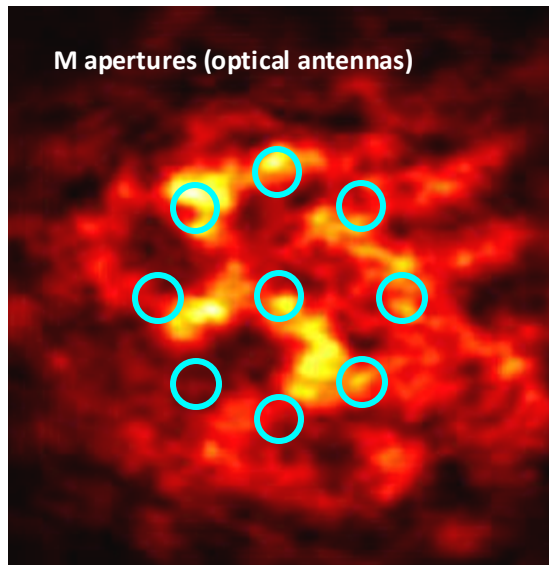
$$\theta_i = 2 \tan^{-1} \left| \frac{x_i}{x_{i+1}} \right|$$

- Combining 2x1 coherent adders, an arbitrary number of inputs signals can be coherently summed
- Calibration strategy: zeroing the power at monitor ports

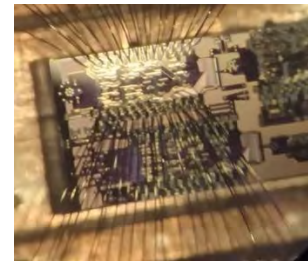
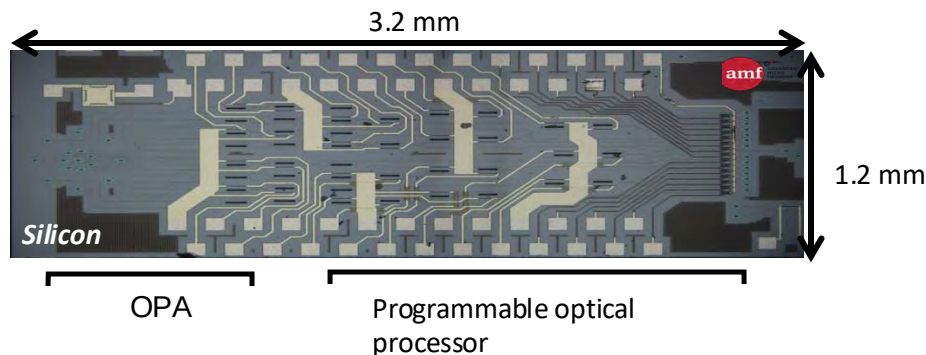
Free Space Optical (FSO) Link



The Optical Analog Processor based receiver



A device capable of coupling an arbitrary free-space beam (*non-spatially coherent* → “*multimode*”) into a specific output beam (*spatially coherent* → “*single-mode*”)



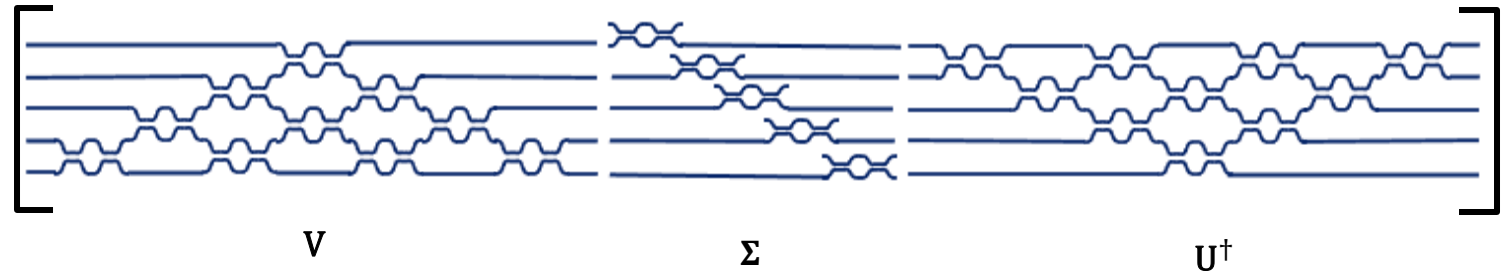
W. Bogaerts, ... F. Morichetti, A. Melloni
Programmable photonic circuits, Nature 586, 207–216 (2020)

Any matrix can be factorized as the product of two unitary matrices $\mathbf{V}$ and $\mathbf{U}$, and a diagonal matrix $\mathbf{\Sigma}$ (singular values)

$$\mathbf{W} = \mathbf{V}\mathbf{\Sigma}\mathbf{U}^\dagger$$

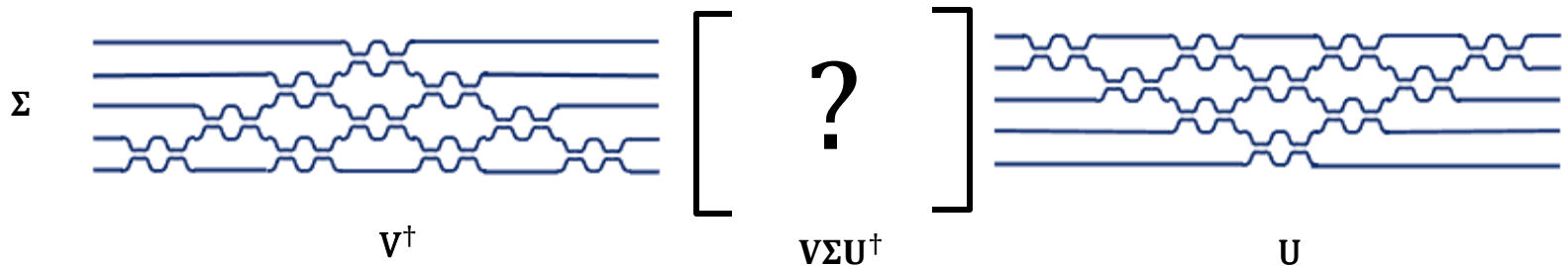
A system of MZI meshes can be used to implement any arbitrary matrix $\mathbf{W}$

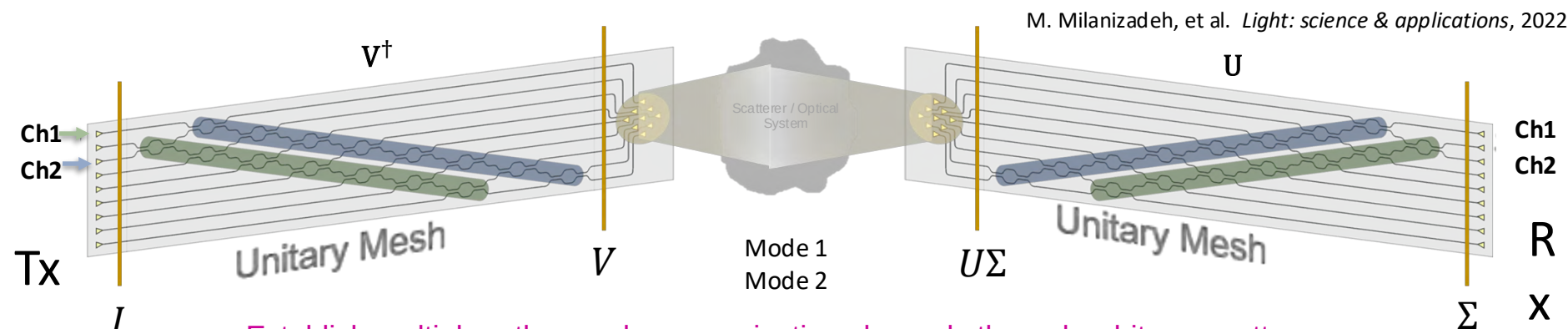
Synthesis:



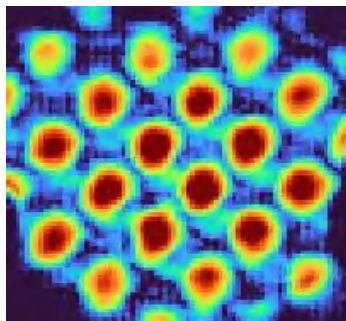
... but also to calculate the SVD of an arbitrary optical system (SVD factorization)

Analysis:

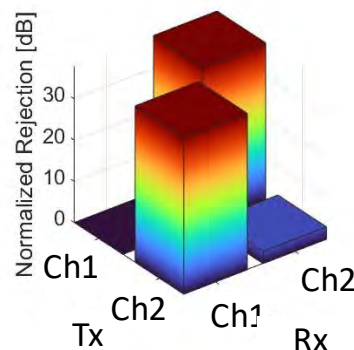
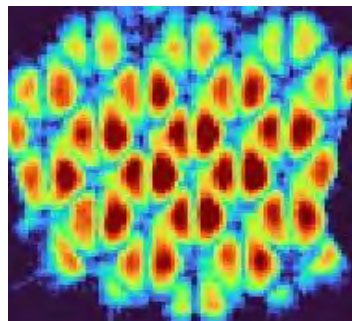




Mode₁

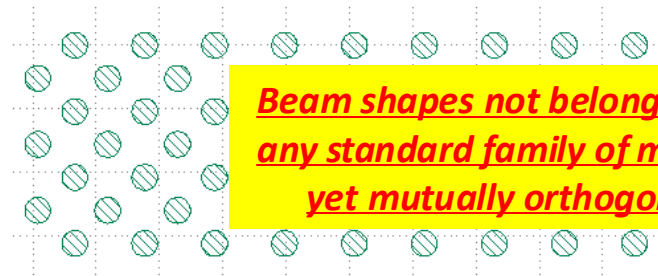
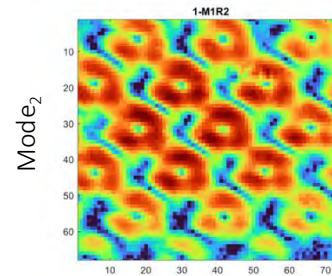
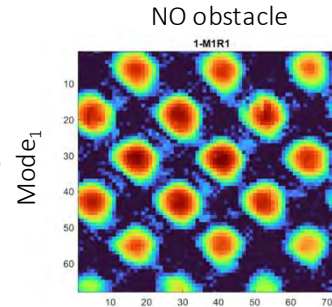
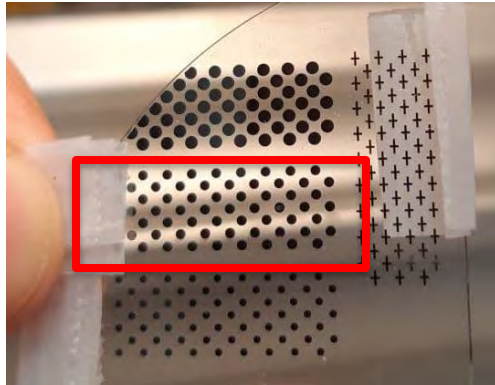
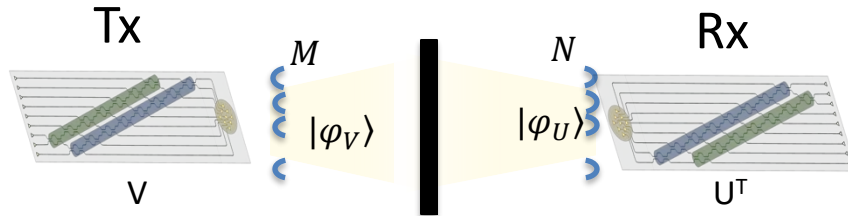


Mode₂

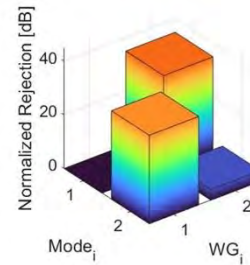


The best FSO
orthogonal modes
 (channels)
 can be found
automatically...

Obstacle in the free-space path



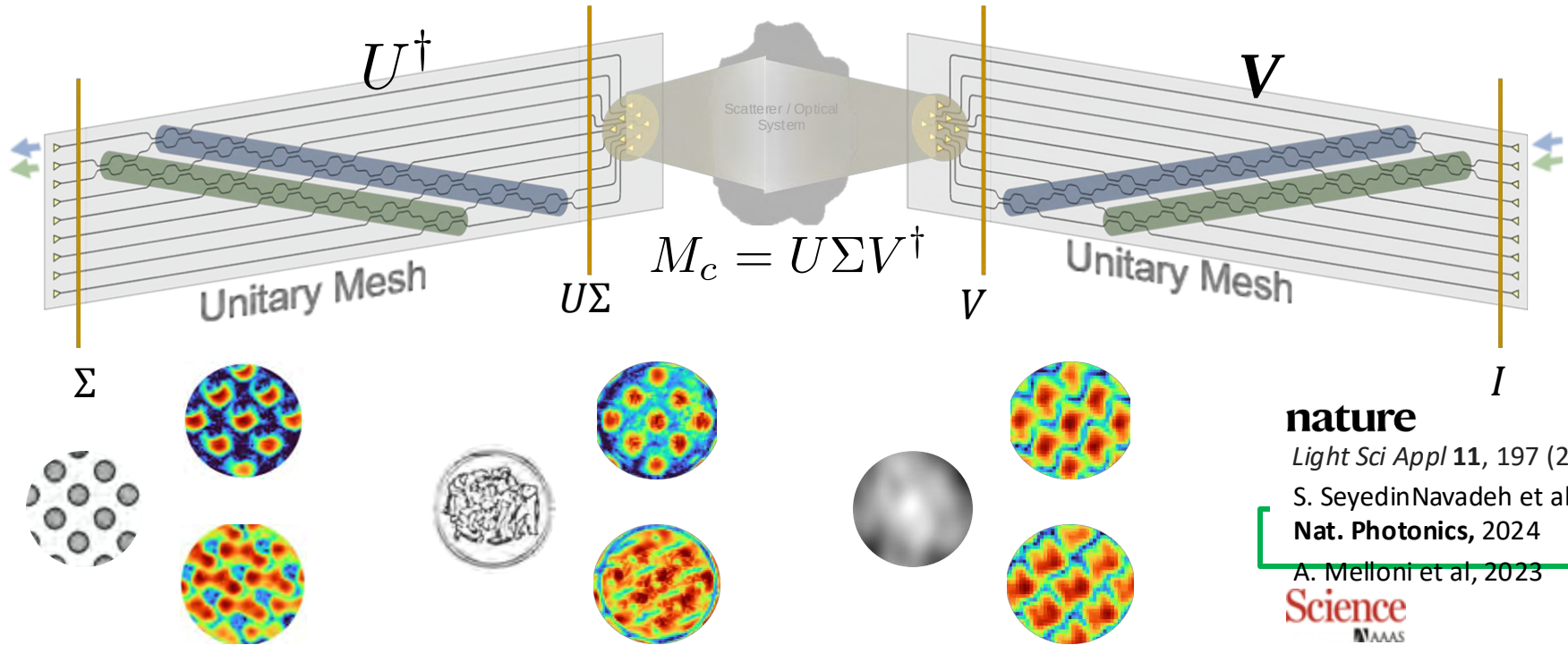
Beam shapes not belonging to any standard family of modes, yet mutually orthogonal



Singular value decomposition



This is a physical implementation of **singular value decomposition (SVD)** of the channel transmission matrix



nature

Light Sci Appl **11**, 197 (2022)

S. SeyedinNavadeh et al.,

Nat. Photonics, 2024

A. Melloni et al, 2023

Science

AAAS

380, 398–404, Apr 2023

Applications: general purpose, Matrix Algebra, mathematical accelerators, convolutional NN, tensor cores,...

